M1.(a) force between two (point) charges is

proportional to product of charges 🗸

inversely proportional to square of distance between the charges 🗸

Mention of force is essential, otherwise no marks.

Condone "proportional to charges".

Do not allow "square of radius" when radius is undefined.

Award full credit for equation with all terms defined.

2

(b) V is inversely proportional to r [or V ∝ (-)1 / r] ✓
 (V has negative values) because charge is negative
 [or because force is attractive on + charge placed near it
 or because electric potential is + for + charge and - for - charge] ✓
 potential is defined to be zero at infinity ✓

Allow $V \times r = constant$ for 1^{st} mark.

max 2

(c) (i) $Q(=4\pi\varepsilon_0 \ rV) = 4\pi\varepsilon_0 \times 0.125 \times 2000$ **OR** gradient = $Q/4\pi\varepsilon_0 = 2000/8$

> (for example, using any pair of values from graph) \checkmark = 28 (27.8) (± 1) (nC) \checkmark (gives Q = 28 (27.8) ±1 (nC) \checkmark

> > 2

(ii) at r = 0.20m V = -1250V and at r = 0.50m V = -500V so pd $\Delta V = -500 - (-1250) = 750$ (V) \checkmark work done $\Delta W (= Q\Delta V) = 60 \times 10^{-9} \times 750$ = $4.5(0) \times 10^{-5}$ (J) (45 μ J) \checkmark

(final answer could be between 3.9 and 5.1 \times 10⁻⁵)

Allow tolerance of ± 50V on graph readings.

[Alternative for 1st mark:

$$\Delta V = \frac{27.8 \times 10^{-9}}{4\pi\varepsilon_0} \times \left(\frac{1}{0.2} - \frac{1}{0.5}\right)$$
 (or similar substitution using 60 nC

instead of 27.8 nC: use of 60 nC gives $\Delta V = 1620V$)]

2

(iii)
$$E\left(=\frac{Q}{4\pi\varepsilon_0 r^2}\right) = \frac{27.8 \times 10^{-9}}{4\pi\varepsilon_0 \times 0.40^2} = 1600 (1560) (\text{V m}^{-1}) \checkmark$$
[or deduce $E = r$ by combining $E = \frac{Q}{4\pi\varepsilon_0 r^2}$ with $V = \frac{Q}{4\pi\varepsilon_0 r} \checkmark$
from graph $E = \frac{625 \pm 50}{0.40} = 1600 (1560 \pm 130) (\text{V m}^{-1}) \checkmark$]
$$Use of $Q = 30 \text{ nC gives } 1690 (\text{V m}^{-1}).$
Allow ecf from Q value in (i).
If $Q = 60 \text{ nC is used here, no marks to be awarded.}$

$$E\left(\frac{Q}{4\pi\varepsilon_0 r^2}\right) = \frac{Q}{4\pi\varepsilon_0 r^2} \checkmark$$
from graph $E = \frac{Q}{4\pi\varepsilon_0 r^2} \checkmark$ with $V = \frac{Q}{4\pi\varepsilon_0 r} \checkmark$
from graph $E = \frac{Q}{4\pi\varepsilon_0 r^2} \checkmark$ with $V = \frac{Q}{4\pi\varepsilon_0 r^2} \checkmark$$$

and inversely proportional to the square of their distance apart <

force between two (point) charges is proportional to (product of) charges ✓

M6.(a)

(b) (i) lines with arrows radiating outwards from each charge ✓ more lines associated with 6nC charge than with 4nC ✓ lines start radially and become non-radial with correct curvature further away from each charge ✓ correct asymmetric pattern (with neutral pt closer to 4nC charge) ✓

3 max

(ii) force
$$\left(= \frac{Q_1 Q_2}{4\pi \varepsilon_0 r^2} \right) = \frac{4.0 \times 10^{-9} \times 6.0 \times 10^{-9}}{4\pi \times 8.85 \times 10^{-12} \times (68 \times 10^{-3})^2}$$

=
$$4.6(7) \times 10^{-5} (N) \checkmark$$

Treat substitution errors such as 10-(instead of 10-) as AE with ECF available.

2

(c) (i)
$$E_4 = \frac{4.0 \times 10^{-9}}{4\pi\epsilon_0 \times (34 \times 10^{-3})^2}$$
 (= 3.11 × 10⁴ V m⁻¹) (to the right) \checkmark

For both of 1st two marks to be awarded, substitution for **either** or both of E_4 **or** E_6 (or a substitution in an expression for E_6 - E_4) must be shown.

$$E_{\epsilon} = \frac{6.0 \times 10^{-9}}{4\pi \epsilon_0 \times (34 \times 10^{-3})^2} = (4.67 \times 10^4 \text{ V m}^{-1}) \text{ (to the left) } \checkmark$$

If no substitution is shown, but evaluation is correct for E_4 and E_6 , award one of 1 st two marks.

$$E_{\text{resultant}} = (4.67 - 3.11) \times 10^4 = 1.5(6) \times 10^4$$

Unit: V m⁻¹ (or N C⁻¹) ✓

Use of $r = 68 \times 10^{-3}$ is a physics error with no ECF. Unit mark is independent.

4

(ii) direction: towards 4 nC charge or to the left ✓

1

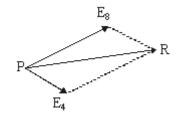
[12] M7. D [1] С M8. [1] M9. D [1] M10. D [1] M11. С [1] **M12**. A

[1]

3

4

- M13. (a) (i) force per unit charge (1) acting on a positive charge (1)
 - (ii) vector (1)
 - (b) (i) $F\left(=\frac{Q_1Q_2}{4\pi\varepsilon_0r^2}\right) = \frac{4.0\times10^{-9}\times8.0\times10^{-9}}{4\pi\times8.85\times10^{-12}\times(80\times10^{-3})^2}$ (1) $=4.5(0)\times10^{-6}\text{N (1)}$
 - (ii) (use of $V = \frac{Q}{4\pi\varepsilon_0 x}$ gives) $0 = \left(\frac{4.0 \times 10^{-9}}{4\pi\varepsilon_0 x}\right) \left(\frac{8.0 \times 10^{-9}}{4\pi\varepsilon_0 (80 \times 10^{-3} x)}\right)$ or $\frac{4}{x} = \frac{8}{80 x}$ (1) x = 26.7 mm (1)
 - (c) correct directions for E₄ and E₈ (1)
 E₈ approx twice as long as E₄ (1)
 correct direction of resultant R
 shown (1)



3 [10]

M14. D

[1]

M15. D

[1]

M16. A

[1]

M17. D

[1]