

## Circuits

## Mark Scheme

Time available: 89 minutes Marks available: 65 marks

## Mark schemes

1. (a) Use of
$V_{0}=\frac{R_{1}}{R_{1}+R_{2}} \times V_{\text {in }}$
OR
$V_{1}: V_{2}=R_{1}: R_{2} \checkmark$
$(R=) 1.7(\Omega) \checkmark$
Alternative MP1:
pd across the variable resistor $=11.25 \mathrm{~V}$
OR
current $=0.45 \mathrm{~A}$
(b) use of $V=I R \checkmark$
$(R=) 4.7(\Omega) \checkmark$
(c) Temperature increases so resistance increases $\checkmark$

Vibration of the lattice ions increases (with temperature) $\checkmark$
More collisions between the (conduction) electrons and the lattice ions (at higher temperature) $\checkmark$
(d) use of $\frac{1}{R_{T}}=\frac{1}{R_{1}}+\frac{1}{R_{2}} \checkmark$
$(R=) 4.8(\Omega) \checkmark$
Alternative MP1:
determines $I_{T}$ current in battery ( $I_{T}=2.48 \mathrm{~A}$ ) and uses $V=I R$
(e) use of $P=\frac{V^{2}}{R} \checkmark$
$(P=) 30(W) \checkmark$
Ecf from (d)
(f) Voltage range is wider 0-12 V (in Figure 4's circuit)

## OR

bulb won't light at lower range so control is unaffected $\checkmark$
Efficiency is less because more power dissipated in Figure 4 (for any particular voltage across the lamp compared to this voltage across the lamp in Figure 2) $\checkmark$

At any voltage across the lamp there is always 12 V across the resistor in Fig 4 which produces heating whereas only the remaining portion of 12 V is across the resistor in Fig $2 \checkmark$
2. (a) The amount of energy is transferred from chemical energy to electrical energy (for every coulomb of charge) $\sqrt{ }$

Alternative first mark:
The work done in moving (1 coulomb of) charge whole way round circuit
5.30 J of energy per coulomb of charge $\sqrt{ }$
(b) $5.30-1.05=4.25(\mathrm{~V})$ seen
or

### 4.25 V across $640 \Omega$ resistor seen

or
use of $V=I R \checkmark$
Allow use of $V=I R$ to find the current in the $320 \Omega$ resistor. ( $I=$ $\left.3.28 \times 10^{-3}(A)\right)$
$\left(I=\frac{4.25}{640}=\right) 6.6(4) \times 10^{-3}(\mathrm{~A})$
Where candidates assume voltmeter has resistance $320 \Omega$, their answer $=6.56 \times 10^{-3} \mathrm{~A}$. Do not credit this.
(c) Use of $V=I R$ seen (finds total resistance of circuit) Or
Use of $V=I R$ for parallel section seen $\checkmark$
$R_{T}=798(\Omega)$ (expect to see $757(7 \mathrm{~mA})$ or $803(6.6 \mathrm{~mA})$ or 807 ( 6.56 mA )
Allow their $R_{T}$ or their total resistance of the parallel section
Use of $R_{T}=R_{1}+R_{2}$ or $\frac{1}{R_{T}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}$ seen (finds resistance of voltmeter) $\checkmark$
$(R=) 312.6(\Omega)$ or $313(\Omega)$ or $310(\Omega)$ seen $\checkmark$

$$
I=3.28 \times 10^{-3}(A)(\text { evidence for this may be seen in }(b))
$$

Alternatively:
Use of $V=I R$ seen (finds current in $320 \Omega$ resistor) $\checkmark$
Allow their $I_{T}$ and their current in the $320 \Omega$ resistor.
Use of $I_{T}=I_{1}+I_{2}$ seen (finds current in voltmeter) $\checkmark$
$(R=) 312.6(\Omega)$ or $313(\Omega)$ or $310(\Omega)$ seen $\checkmark$
Answer is:
$316 \Omega$ where $I=6.6 \mathrm{~mA}$
$282 \Omega$ where $I=7 \mathrm{~mA}$
$320 \Omega$ where $I=6.56 \mathrm{~mA}$
Must see working to support their answer.
No workings = zero marks.
(d) Use of $P=V^{2} / R \checkmark$

Allow their $V$ along with $R$ from part (c)
Allow $V=5.3$ with their $R$
Alternative $1^{\text {st }} \mathrm{MP}$
Use of $V=I R$ and $P=I^{2} R$ or
$V=I R$ and $P=V I \checkmark$
( $P=$ ) $0.090(\mathrm{~W}) \checkmark$
Answer $=0.094$ (W) where $R=300 \Omega$
Condone 1 sf answer where $R=300 \Omega$ is used.
(e) Current in circuit changes (as voltmeter position changes) / ratio of the voltage dropped across each resistor changes as voltmeter position changes. $\checkmark$

Because resistance in the circuit decrease / changes $\sqrt{ }$
Allow maximum of 1 mark for the reading will only be the emf if the voltmeter is across both resistors.
3. (a) $\quad R_{\text {LDR }}$ without light $=300 \mathrm{k} \Omega \checkmark$
$I=\frac{V}{R}=\frac{5}{310 \times 10^{3}}=16.1 \times 10^{-6} \mathrm{~A} \checkmark$
Allow ecf for their $R$
(b) $V$ with without light $=I R=16.1 \times 10^{-6} \times 300 \times 10^{3}=4.84 \mathrm{~V} \checkmark$
ecf from (a)
Allow 92-100 k
With light $V=\left(\frac{93}{93+10}\right) \times 5.0=4.51 \mathrm{~V}$ V
Conclusion and calculate of change in voltage and comparison with $1.25 \mathrm{~V} \checkmark$
$4.8-4.5=0.3 \mathrm{~V}$ so no.
Allow 1 sf (allow ecf)
4. (a) Work done in moving 1 C of charge through the cell $\checkmark$ 1.5 J of work is done in moving 1 C of charge through the cell $\checkmark$

OR
Amount of energy converted from other forms to electrical energy per 1 C of charge $\checkmark$
1.5 J of energy converted from other forms to electrical energy per unit charge (passing across the emf) $\checkmark$

OR
Work done in moving 1 C of charge (whole way) round circuit $\checkmark$
1.5 J of work is done in moving 1 C of charge the (whole way) round circuit $\checkmark$
$2^{\text {nd }}$ marking point obtains both marks
Max 1 mark available for the following:
The emf is the terminal pd when there is no current in the cell (and this equals 1.5 V )
1.5 J of energy per 1 C of charge.

Allow a statement of Kirchhoff's 2 nd law for 1 mark. Where the law is in symbol form, the meaning of the symbols must be stated. Need a clear communication of internal and external resistances.
(b) $\mathrm{P}=\mathrm{VI}$

And
$(\mathrm{P})=0.465(\mathrm{~W}) \checkmark$
Seen to more than 2 sf with supporting equation with subject seen in working
(c) Use of appropriate power equation to determine wasted power or
power dissipated in $\mathbf{R}=$ total power - their wasted power $\checkmark$
( $P=$ ) 0.40 W $\checkmark$
Alternative for 1 mark:
Use of $I=\frac{\varepsilon}{R+r}$
Or
pd across $R=1.5-0.65 \times 0.31$
or
pd across $R=1.2985$ (V)
or
total resistance $=1.5 / 0.31$
or
total resistance $=4.839(\Omega)$
or $R=4.2(\Omega)$
or $P=I^{2} x$ their $R$
or
$P=\frac{V^{2}}{R}$ using their $V$ and $R \checkmark$
(d) Use of $E=P t$
or $E=V I t$
Or
$E=Q V$ and $Q=I t \checkmark$
Allow use of the equation with their values.
An answer of $3.5 \times 10^{4}$ is worth 1 mark
$(t=) 3.0(1) \times 10^{4}(\mathrm{~s}) \checkmark$
(e) MAX 3 from ( $\mathbf{1}$ to $\mathbf{4}$ ) or (5 to 8)

It is suitable, because:
(1) Current required in lamp $=0.62 \mathrm{~A}$ or use of $\mathrm{I}=_{V}^{P}$ seen
(2) Resistance of lamp $=2.11 \Omega$ or use of $R=\frac{V^{2}}{P}$ seen $\checkmark$
(3) current in each cell $=0.31 \mathrm{~A} \checkmark$
(4) lost volts $=0.2 \mathrm{~V}$
or
lost volts $=0.65 \times 0.31 \mathrm{~V}$
Check the diagram in part (e)
Must have the correct conclusion to award 4 marks.
Conclusion: yes, terminal $p d=1.5 \mathbf{- 0 . 2}$ seen
or
terminal pd=1.5-0.65 $\times 0.4 / 1.3 \checkmark$
OR
(5) total internal resistance $=0.325 \Omega \checkmark$
(6) total resistance in circuit $=2.44 \Omega \checkmark$
(7) Resistance of lamp $=2.11 \Omega \checkmark$
(8) pd splits in ratio of 0.325:2.11 $\checkmark$

Conclusion: yes, pd across lamp is $\frac{2.11 \times 1.5}{2.44}(=1.3 \mathrm{~V})$ seen $\checkmark$
Allow max 3 from a combination of two route [(2) and (7) worth total of 1 mark]
(e) (Cells must be added) in parallel $\checkmark$

Because:
more energy stored in the bank of cells / less power from each cell $\checkmark$
without increasing the voltage across the bulb (above 1.5 V )
or
without increasing the terminal pd (above 1.5 V ) $\checkmark$
Must link the cells being added in parallel to one or both reason to gain three marks.
Alternative:

- In parallel
- Current shared by cells
- Takes longer to convert the energy stored in each cell.

Alternative:

- In parallel
- Less internal resistance
- Less power / energy wasted

Cells in series statement means no marks can be obtained.
5. (a) Mention of increase in lost volts/ pd across internal resistance (in cell) $\checkmark$ (because) current has increased

OR
internal resistance is a larger proportion of total resistance OR
ratio of internal: external resistance is larger $\checkmark$
Accept reverse arguments
Do not accept terminal pd has decreased
Treat comments about resistance of lamp as neutral
(b) Lost volts reduced (current remains the same, V2 > V1)

## OR

Effective internal resistance is a smaller proportion of total resistance / ratio of internal: external resistance is smaller $\checkmark$
(because)
two cells in parallel behave as a single cell (with the same emf) but with half the internal resistance / reduced internal resistance $\checkmark$

## Alternative:

Current through each cell is less than cell on its own $\checkmark$
Decreased current through cell decreases lost volts / pd dropped across internal resistance $\sqrt{ }$
6. (a) valid continuous series circuit that includes ammeter, and one wire link (condone diagonal connections)
and
voltmeter between any two sockets that enable the terminal pd to be measured $\checkmark$ all of the following are acceptable:

links and connections
reject broken / dashed lines
tolerate diagrams with diagonal or non-straight connections between sockets if these will produce a valid circuit
don't insist on connection blobs
circuit must be continuous unless a switch is included: otherwise no gaps wider than the thickness of their links inclusion of a switch is neutral but the length of the open switch must be $\geq$ length of the gap where the switch is connected: condone the whole gap between terminals vertically opposite the ammeter to be marked as an open switch

## meters

correct ASE symbol for ammeter and correct ASE symbol for voltmeter are essential
one voltmeter and one ammeter only
meters must not be 'transparent'
positions of meters assume that the ammeter has negligible resistance and voltmeter has infinite resistance
(b) (with any switch closed) read ammeter and voltmeter
or
record / measure $I$ and $V$;
adjust / vary / change resistance / (setting of) variable resistor / Q
and repeat (readings) $1 \checkmark$
for $1 \checkmark$ must produce a range of $I, V$ values ( $>2$ sets) and identify how this is achieved; it is not necessary to suggest range or number of sets
plot $V$ (against) $I 2 \checkmark$
mark $2 \checkmark$ independently of $1 \checkmark$
$\varepsilon=$ (vertical $/ y$-axis) intercept $3 \checkmark$
$r=-$ gradient $4 \checkmark$
$2 \sqrt{ } 3 \sqrt{ }$ and $4 \sqrt{ }$ can be awarded for a suitable sketch graph
condone 'use the (variable) resistor to vary current and read $I, V$ ' idea that $R$ can be read from $Q$ is neutral
for $2 \checkmark$ (and further credit in $3 \checkmark$ and $4 \checkmark$ ) the ordinate and the abscissa must be identified;
allow 'plot V over I ' or 'plot V/I'
allow $2 \checkmark$ for reverse plot 'I (against) $V$ '
then $4 \checkmark$ for $r=r=\frac{-1}{\text { gradient }}$ and $3 \checkmark$ intercept $=\frac{\varepsilon}{r}$
for $3 \checkmark$ open circuit methods involving $\varepsilon$ read directly using voltmeter are neutral
for $4 \sqrt{ }$ any subject but minus sign essential
variation
$1 \sqrt{ }$ as above;
$3 \sqrt{ }$ find $R$ from $V$ divided by $I$; disconnect external circuit and
measure $\varepsilon$ directly;
$4 \checkmark$ plot $\frac{\varepsilon}{V}$ against $\frac{1}{R}$
$2 \sqrt{ }$ gradient $=r$
(c) gradient calculation seen with $\Delta n^{-1}$ divided by $\Delta I^{-1}$;
$\varepsilon$ from $22 \times$ gradient $1 \checkmark$
for $1 \checkmark$ do not penalise one read off error, (allow use of 0,0 ) or for small steps
expect gradient $\approx 7.2(5) \times 10^{-2}$ leading to $\varepsilon=1.594(\mathrm{~V})$
do not allow reverse working based on answer to part (e)
$\varepsilon$ minimum 3 sf; in range 1.58 to $1.61(\mathrm{~V}) 2 \sqrt{ }$
$2 \checkmark$ is contingent on award of $1 \checkmark$
(d) use of Figure 3 to read off $I^{-1}$ corresponding to $n^{-1}=0.25$;
calculates $I$ in range $0.23(2)$ to $0.24(4)(\mathrm{A}) \checkmark$ do not insist on seeing evidence of working on Figure 3 expect $I^{-1}=4.2 \pm 0.1\left(A^{-1}\right)$ leading to $I=0.238$ (A) (should expect 1 more sf than in 0.25 for 'show that' but condone 0.23 and 0.24 since result based on 2 sf data) do not allow reverse working based on answer to (e)
(e) circuit resistance $R=5.5(\Omega)$ seen in (e) working $1 \checkmark$
minimum 2 sf $V$ from their $I \times 5.5$
or
$V$ from their $\varepsilon$ - their $I \times r 2 \sqrt{ }$

$$
\begin{aligned}
& \text { for } 1 \sqrt{ } \text { allow } R=R=\frac{22}{4} \text { or } \frac{11}{2} ; \text { allow } R^{-1}=R^{-1}=\frac{4}{22} \text { etc } \\
& \text { for } 2 \sqrt{ } \text { correct } R \text { only; expect } V=1.3(1) V \text {; use of } I=0.25 \mathrm{~A} \text { gives } V \\
& =1.38 \mathrm{~V} \\
& \text { do not allow } V \geq \text { their } \varepsilon
\end{aligned}
$$

$r$ using lost volts divided by current; full substitution of their valid data
eg $r=\frac{1.58-1.31}{0.238} 3^{v}$
or
$r$ using formula for Figure 3; full substitution of their valid data
eg $r=\frac{\varepsilon}{I}-\frac{22}{4}=\frac{1.58}{0.238}-5.53 \quad$
or
$r$ using either intercept on Figure 3; full substitution of their valid data
eg their vertical intercept $\times-22$ or
their horizontal intercept $\times \varepsilon 3 \checkmark$
use of 'show that' or 2 sf data:
$r=\frac{\varepsilon-V}{I}$ with $\varepsilon=1.6 \mathrm{~V}, \mathrm{~V}=1.4 \mathrm{~V}$ and
$I=0.25$ A gives $r=0.80 \Omega$
$\frac{22}{n}=\frac{\varepsilon}{I}-r$ with $\varepsilon=1.6 \mathrm{~V}, I=0.25 \mathrm{~A}$
and $n=4$ gives $r=0.90 \Omega$;
(can find $r$ first, then $V$ using $\varepsilon$ - Ir)
a vertical intercept must be calculated; result is negative, eg vertical intercept $=-0.053$ :
$r=-1 \times-0.053 \times 22=1.17(\Omega)$
horizontal intercept $=0.73$ :
$r=1.6 \times 0.73=1.18(\Omega)$
minimum 2 sf result in range 0.80 and $1.3(0)(\Omega) 4 \checkmark$ allow $4 \sqrt{ }$ only if there is clear evidence of a valid method leading to a result in range
$n=2$ and $n=31 \checkmark$
$n=5$ or $n=6$ or $n=72 \sqrt{ }$
to improve distribution of points (along the line) or wtte $3 \boldsymbol{\checkmark}$
for $1 \sqrt{ }$ and $2 \sqrt{ }$ if suggesting more than three values for $n$ accept only the last three
for $3 \sqrt{ }$ allow:
'spread out' / 'avoid concentrating' points'
where current / $n$ is smaller' or wtte 'reduce distance between points (data)' / (add) detail
'most uniform distribution' / 'most equally spread out' / 'roughly evenly spaced'
reject:
'making points (data) 'equally' / 'evenly-spaced'/ 'even spread' (without qualification)
'easier to plot / draw line' / 'line more accurate'/ 'easier to see trend' are neutral
(h) both points move (by $\geq$ half a grid square) to the right $1 \checkmark$
both points move (by $\geq$ half a grid square) causing the gradient of a straight line between them to be reduced $2 \sqrt{ }$
allow badly-marked points / use of arrows
ignore any best-fit line added to Figure 5
for $1 \checkmark$ rightwards motion of each point must be parallel to gridlines $\pm$ half small square
award of $2 \sqrt{ }$ mark is independent of $1 \checkmark$ mark
for $2 \sqrt{ }$ the points do not need to move in the same direction

