##  <br> <br> A-Level Physics <br> <br> A-Level Physics <br> Ideal Gases <br> Mark Scheme

Time available: 75 minutes Marks available: 49 marks

1. (a) Any two from $\checkmark \checkmark$

- Volume of molecules is negligible compared to that of the container
- Collision time is negligible or small compared to the time between collisions
- Collisions are elastic or kinetic energy is conserved
- There are negligible forces between molecules (except during collisions)
- Newtonian mechanics apply
(b) ( NI ) molecules do not maintain a constant velocity (when hitting the walls) so they must experience a force. $\checkmark_{1}$ owtte.
(NII) Molecules have a rate of change of momentum when bouncing off the walls and force =/is related to rate of change of momentum.
$\checkmark_{2}$
owtte.
(NIII) A force is exerted by the wall on the molecules so the molecules exert a force on the wall. $\sqrt{3}$
owtte
For each mark the essence of the Newton law must be given in the context of the gas.
Just quoting a Newton law is not enough for a mark.
$\checkmark{ }_{2}$ 'rate of change' must be used.
(c) Use of $E_{\mathrm{k}}=\frac{3}{2} \mathrm{k} T$ to find a temperature $\checkmark_{1}$

$$
\left(T=\frac{2 \times}{3 \times} \times \frac{6.7 \times 10^{-21}}{1.38 \times 10^{-23}}=324 \mathrm{~K}\right)
$$

Use of $P V=n R T$ with calculated temperature $\checkmark_{2}$
$\left(n=\left(\frac{P V}{R T}=\frac{220 \times 10^{3} \times 0.35}{8.31 \times 324}\right)\right)$
amount of gas $=29(\mathrm{~mol}) \sqrt{3}(28.6 \mathrm{~mol})$
$\checkmark_{1}$ for rearranged equation with data that may have powers of 10 or transcript errors with constants as symbols. A temperature answer is needed or the fully substituted equation.
$\checkmark_{2}$ for rearranged equation with data that includes the calculated temperature and may have powers of 10 or simple transcript errors with constants as symbols $\sqrt{ }$ no ecf, correct answer only
(d) Drawn graph with concave shape passing through at least one of the data points. (data points are shown as crosses on the graph) $\checkmark$

Passing through coordinates $(2,8),(4,4)$ and $(8,2) \checkmark$ (coordinates refer to cm intervals on the graph)

Drawn line must be within a small square ( 2 mm ) of a data point to count.

2. (a) attempts two calculations that would lead to a conclusion ${ }_{1} \checkmark$
for ${ }_{1} \checkmark$ the result of at least one calculation of $M \times y$ must be correct (see table) otherwise withhold both marks;
allow use of $y$ in $m$ but reject POT error
a reasoned judgement explaining why $y$ not inversely proportional to $M_{2} \sqrt{ }$

| $\boldsymbol{M} / \mathbf{k g}$ | $\boldsymbol{y} / \mathbf{m m}$ | acceptable $\boldsymbol{M} \times \boldsymbol{y}$ | $\mathbf{m i n} \mathbf{s f}$ |
| :---: | :---: | :---: | :---: |
| 0.5 | $89(.0)$ | $44.5 / 45$ | 2 |
| 1.0 | $82(.0)$ | $82(.0)$ |  |
| 1.5 | $76(.0)$ | $114(.0)$ |  |
| 2.0 | $71(.0)$ | $142(.0)$ | 3 |
| 2.5 | 66.5 | $166(.3)$ |  |
| 3.0 | 62.5 | $187.5 / 188$ |  |

for ${ }_{2} \sqrt{ }$ two correct calculations of $M \times y$; see table for min sf in result for $M \times y$
OR
one correct calculation of $M \times y$ and an appropriate reverseworking calculation;
statement rejecting inverse-proportion supported by suitable quantitative reasoning, eg calculation of the percentage difference between the results of their calculations;
condone weaker 'large' / 'significant differences’ (between calculation results);
reject 'values are different' / 'not constant' / 'not close enough' reasoning must be based on the data points, eg reject 'best-fit line crosses $y$-axis'
for ${ }_{12} \sqrt{ }$ condone use of two rows of data to show that when $M$ doubles, $y$ does not halve
(b) (as $\mathbf{P}$ moves down) trapped air expands ${ }_{1} \checkmark$
(so) pressure of trapped air is reduced ${ }_{2} \sqrt{ }$
pressure of trapped air becomes less than atmospheric pressure ${ }_{3} \checkmark$
pressure difference across $\mathbf{P}$ produces upwards force which balances weight of $\mathbf{P}_{4} \boldsymbol{\checkmark}$
pressure difference across $\mathbf{P} \times$ area of piston $=$ weight of piston ${ }_{5} \checkmark$
for ${ }_{1} \checkmark$ allow 'volume (of trapped air) increases' / 'is less compressed'
for ${ }_{3} \sqrt{ }$ reject 'atmospheric pressure constant'
for ${ }_{4} \sqrt{5} \checkmark$ allow any correct idea of equilibrium being achieved
(c) smooth curve of decreasing negative gradient through all 6 points ${ }_{1} \checkmark$
curve extrapolated (backwards) to $M=-0.7_{2} \sqrt{ }$
(clear evidence that) value of $y$ corresponding to $M=-0.7$ read off $\sqrt{ } \checkmark$
$y$ in range 110 mm to $114 \mathrm{~mm}_{4} \sqrt{ }$
OR
for incorrect method
curve extrapolated (backwards) to $M=-0.35$ and (clear evidence that) value of $y$ corresponding to $M=-0.35$ has been read off ${ }_{23} \checkmark$
$y$ in range 103 mm to $105 \mathrm{~mm}_{4} \sqrt{ }$
withhold ${ }_{1} \checkmark$ for any linear region and annotate clip to explain condone poorly-marked line but insist that line passes through all 6 points
for ${ }_{3} \sqrt{ }$ 'clear evidence' means a plausible answer for $y$ clearly obtained by the correct method or suitable working shown on Figure 2

(d) correctly identifies error ${ }_{1} \checkmark$
for ${ }_{1} \sqrt{ }$ reading has been taken from the top of the meniscus / should have been taken from the bottom of the meniscus
correct reading is $35.8_{2} \sqrt{ }$
reject 'sub-divisions are $0.1 \mathrm{~cm}^{3}$ not $0.2 \mathrm{~cm}^{3}$
for ${ }_{2} \sqrt{ }$ CAO 1
(e) gradient evaluated as decimal number to $\geq 2$ sf from valid method ${ }_{1} \checkmark$ for ${ }_{1} \checkmark \Delta \log \left(V / \mathrm{cm}^{3}\right)$ divided by $\Delta \log (P / \mathrm{MPa})$; graph in Figure 5 has gradient of -1.03(3);
states gradient result $\approx-1{ }_{2} \sqrt{ }$
significance explained ${ }_{3} \checkmark$
for missing - sign allow ${ }_{12} \sqrt{ }=1$ MAX
for ${ }_{3} \checkmark$ use of $y=m x+c$ expected; - sign essential
eg $\log V=-\log p+\underline{\text { constant }}$
do not insist on $V=$ constant $\times p^{-1}$

$$
\text { for }{ }_{1} \sqrt{ } \log 0.34=-0.4685
$$

use of at least one other value of $p$ and corresponding $V$

OR
$\log p$ and corresponding $\log V_{2} \checkmark$
solves for unknown $V$;
$\geq 3$ sf result in range 10.5 to $11.5\left(\mathrm{~cm}^{3}\right)$
OR
$11\left(\mathrm{~cm}^{3}\right)_{3} \checkmark$
for ${ }_{2} \checkmark$
check their $p \times V$ in range 3.65 to 3.80
OR
their $\log p+\log V=4.50$ to 6.30
expect
$p_{1}, V_{1}$ values derived from a point on the line in Figure 5; use of $p_{1} V_{1}=p_{2} V_{2}$; sub of $p_{2}=0.34 \&$ solve for $V_{2}$
OR equivalent based on $\log \frac{p_{1}}{p_{2}}=\log \frac{V_{2}}{V_{1}}$
for use of $\ln 0.34=-1.079$ leading to $(\ln V=1.665$ and) $V 23 \checkmark$
(g) temperature (of air) $\sqrt{ } \checkmark$ for ${ }_{1} \checkmark$ accept 'mean ke of air molecules', 'vapour pressure of air'
change the pressure of the gas slowly or wtte OR
wait until the oil level stabilises ${ }_{2} \checkmark$
for ${ }_{2} \sqrt{ }$ condone 'keep lab temperature constant';
reject 'do not heat the apparatus' / 'keep windows closed' etc
OR
keep purity of oil constant ${ }_{1} \checkmark$
choose oil with low evaporation rate ${ }_{2} \checkmark$
3. (a) (If not in a vacuum) gas atoms will collide with air atoms, changing their direction or speed distribution. $\checkmark$

There must be some indication of a change of the oven gas molecules associated with collisions
If temperature change is mentioned this must be related to speed distribution for the mark
(b) Finds time taken for one rev AND/OR time for $1 / 8$ rev $\checkmark$
(Uses speed = distance/time to get)
$=0.500 / 1.04 \times 10^{-3}=480 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
(so about $500 \mathrm{~m} \mathrm{~s}^{-1}$ )
1 rev in $1 / 120$ s or 0.00833 s
Time for $45^{\circ}$ or $1 / 8 \mathrm{rev}=1.04 \times 10^{-3} \mathrm{~s}$
Must have 2 or more sf answer but $500 \mathrm{~m} \mathrm{~s}^{-1}$ is acceptable as a final answer provided the calculated time for 45 or $1 / 8 \mathrm{rev}$ is shown and rounded down to 2 sf
(c) Mass of one atom $=m=0.209 / N A=3.47 \times 10^{-25} \mathrm{~kg} \checkmark_{1}$
$\checkmark_{1}$ May be seen in the substitution of the equation that follows
$\checkmark_{2} \frac{m}{3 k}(\text { answer }(b))^{2}$
Substitutes $m$ and answer (b) in $1 / 2 m\left(c_{\mathrm{rms}}\right)^{2}=\frac{3}{2} k T k T$ and rearranges $\sqrt{2}$

$$
\begin{aligned}
& T=1930 \mathrm{~K} \checkmark_{3} \\
& \qquad \begin{array}{l}
\checkmark_{3} \text { Accept } 2095 \mathrm{~K} \text { or } 2100 \mathrm{~K} \text { if } 500 \mathrm{~m} \mathrm{~s}^{-1} \text { used } \\
\\
\text { A correct answer also gains the second mark }
\end{array} .
\end{aligned}
$$

(d) (Pressure is due to collisions of atoms with oven walls) With fewer atoms fewer collisions per second $\checkmark_{1 a}$
$\checkmark{ }_{1 a}$ There must be a reference to frequency or rate of collision
but average momentum change per collision stays the same or
therefore the total momentum change per second falls (so pressure drops) $\checkmark_{2 \mathrm{a}}$
OR
Reference to $p V=\frac{1}{3} N m\left(c_{r m s}\right)^{2} \checkmark_{1 \mathrm{~b}}$
$c_{r m s}$ is constant as $T$ is constant hence $p \checkmark N$ (so pressure drops) $\checkmark_{2 \mathrm{~b}}$
$\checkmark{ }_{1 b}$ The equation may be in any equivalent kinetic theory form $p V=n R T$ is not acceptable unless a connection is made between $T$ and $c_{r m s}$
(e) $(p V=n R T)$
leaked $n=\frac{V\left(p_{1}-p_{2}\right)}{R T} \checkmark$
$=8.42 \times 10^{-3} \mathrm{~mol}$
ecf for $T$ from (c)
(f) At higher temp atoms will be faster (so drum will not have turned as far) $\checkmark_{1 \text { a }}$

Darkest area will be closer to $A \checkmark_{2 a}$
$\checkmark_{1}$ Accept drawing but allow any degree of maximum darkness.
The drawing may be flat or curved.
B
A

Allow
more atoms will pass through $S$ as it passes the oven, for the first mark
making the dark patch darker, for the second mark. This must be linked to the more atoms
4. (a) Total energy supplied $(=P t)=12 \times 890=10680(\mathrm{~J}) \checkmark_{1}$ $\checkmark_{1}$ Substitution or answer.

Heat energy to evaporate nitrogen at its boiling point $(=\mathrm{ml})=0.05 \times 2.0 \times 105=10$ 000 (J) $\mathfrak{V}_{2}$
$\checkmark{ }_{2}$ Substitution or answer.
(Use of $Q=m c \Delta \theta$ )
Attempt to use $c=\left(\frac{Q}{m \times \Delta \theta}\right)=\frac{(10680-10000)}{0.050 \times(77-70)} \checkmark_{3}$
$\sqrt{3}$ Allow any attempt at substitution with (77-70) or 7 correct but $\Delta Q$ does not have to be correct so can even show an addition.
specific heat capacity of liquid nitrogen $=$
$c=1.9 \times 10^{3} \checkmark_{4}$ (allow 1 sig fig due to the small temperature difference)
$\checkmark_{4}$ Allow 1 sig fig due to the small temperature difference. No ecf correct answer only.
$\mathrm{Jkg}^{-1} \mathrm{~K}^{-1}$ or $\mathrm{Jkg}^{-1}{ }^{\circ} \mathrm{C}^{-1} \checkmark_{5}$ \{taken from the answer line but if not present can come from the body of the answer space\}
$\checkmark_{5}$ Correct answer Consistent with 4th mark and only in the form shown ie no double or single solidus/oblique lines.

Only penalise the kelvin unit if it has an obvious loop at the top allow if simply small.
(b) (Use of volume $=\frac{m}{\rho}$ )
nitrogen gas $=\frac{0.050}{3.8}=0.013\left(\mathrm{~m}^{3}\right) \checkmark_{1}$ \{if both given both must be correct\} $\checkmark 1$ Substitution or answer and can be seen without label or explanation.
nitrogen liquid $=\frac{0.050}{810}=0.000062\left(\mathrm{~m}^{3}\right)$
OR
a reference to the volume being negligible $\sqrt{2}^{2}$
$\checkmark{ }_{2}$ Substitution or answer or words.
Work done in expanding $(=X=p \Delta V)$ $=1.0 \times 10^{5} \times 0.013=1.3 \times 10^{3}(\mathrm{~J}) \sqrt{3}$
$\checkmark{ }_{3}$ Evidence of $\Delta V$ or calculation introduced with 'work done $=$ ' is required for the mark.
For an ecf the product must be shown in full with the substitution of the ecf being clear.
which is less than $1.0 \times 10^{4} \mathrm{~J} /$ the energy to change state $=\mathrm{Y}($ ie $\mathrm{X}<\mathrm{Y}) \checkmark_{4}$ $\checkmark_{4}$ Allow ecf from part (a) for this mark provided the statement is consistent with the figures.
OR
If the ecf comes from the 3rd mark above then the work done in expanding must be clearly labelled for the comparison or have units of Ji.e it cannot be compared with a number that just happens to be on the page.

