

# Motion Along a Straight Line 

## Mark Scheme

Time available: 65 minutes Marks available: 47 marks

1. (a) (component of total weight parallel to slope =) $640 \sin \theta \checkmark$

Allow $m g \sin \theta$ or $65 g \sin \theta$
(b) use of $P=F v \checkmark$
$(\theta=) 17\left({ }^{\circ}\right) \checkmark$
Ecf from (a)
Alternative MP1:
Determines work done in one second
$310=m g h$ giving $h=0.486$
and
determines the distance travelled along the slope of the hill $=1.63$
OR
Use of
$\sin \theta=\frac{\text { height gained per second }}{\text { distance travelled per second }}$
(c) Gains less height every second $\checkmark$

Gains less potential energy every second $\checkmark$
Less useful power output $\sqrt{ }$
Alternatives:
Force applied acts over a greater distance for the same change in height $\checkmark$
Less force required $\checkmark$
Less power output required $\checkmark$
OR
Same gain in GPE requires same gain in height $\checkmark$
Takes longer time to gain height as greater distance to travel $\checkmark$
Less power output $\checkmark$
OR
Effective $\theta$ has decreased $\checkmark$
$m g \sin \theta$ has decreased $\checkmark$
less power output $\checkmark$
OR
The component of the velocity parallel to the slope has decreased $\checkmark$
$P=F v \cos \theta$ has decreased $\checkmark$
Less power output $\checkmark$
General marking principle:
MP1 basic point / MP2 consequence (in terms of energy) / MP3 less power
(d) Draws tangent to curve at $t=10 \mathrm{~s} \checkmark$

Attempts to determine gradient of tangent $\checkmark$
(acceleration $=$ ) $0.21\left(\mathrm{~m} \mathrm{~s}^{-2}\right) \checkmark$
Accept answers in range 0.16 to $0.26\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$
(e) Air resistance increases with speed $\checkmark$

And
MAX 3 from:
Initially, all energy transferred (per sec) to kinetic energy of cyclist $\checkmark$
As speed increases energy transferred (per second) to kinetic energy of cyclist decreases $\checkmark$

As speed increases energy transferred (per second) to the air increases $\checkmark$
At top speed energy transferred (per second) is transferred to air $\checkmark$
2. (a) $\quad(a=) 9.81 \sin 30=4.9\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$ seen $\checkmark$

Allow $g \sin 30$
(b) Substitutes into $v^{2}=u^{2}+2$ as eg $v^{2}=2 \times 5 \times 0.3$

OR
Uses $\frac{v^{2}}{2}=g 0.3 \cos 60 \checkmark$
$1.7\left(\mathrm{~m} \mathrm{~s}^{-1}\right) \checkmark$
(c) Attempt to find area between $0.35 \mathrm{~s}(\mathbf{B})$ and $0.80 \mathrm{~s}(\mathbf{C}) \checkmark$
$395 \pm 25(\mathrm{~N} \mathrm{~s}) \checkmark$
(d) Reads duration from $\mathbf{C}$ to $\mathbf{D}$ from graph: 0.61 or 0.62 (s) $\checkmark$

Uses $s=\frac{1}{2} a t^{2} \mathrm{OR}_{s=\frac{1}{2}(u+v) t \checkmark}$
0.46 or 0.47 (m) $\checkmark$

Condone 9.81 for $a$.
Expect to see $u=1.52\left(\mathrm{~m} \mathrm{~s}^{-1}\right)$ in $s=\frac{1}{2}(u+v) t$
(e) Reads resting force from graph $=360 \mathrm{~N}$ OR divides an incorrect reading by $5(4.91 \mathrm{~N} / \mathrm{kg}) \checkmark$
$72(\mathrm{~kg}) \checkmark$
3. (a) (Work done $=$ lost $\left.K E=1 / 2 m v^{2}=\right) 0.019(J) \checkmark$
(b) Use of $W=F s \checkmark$

Condone POT error in substitution
ECF from (a)
Alternative:
Use of an appropriate suvat equation and use of $F=m a \checkmark$
$\left(t=9.8 \times 10^{-6} \mathrm{~s}\right)$
( $a=6.0 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-2}$ )
Condone POT error in substitution
No ECF from 3.1 this route $(F=) 0.66(N) \checkmark$

## $(F=) 0.66(N) \checkmark$

(c) Use of Volume $=$ Thickness $x$ area of cross-section $\checkmark$

Condone POT errors apart from final answer ( $V=$ ) $8 \times 10^{-4} \times 0.03$ $\operatorname{Or}(V=) 2.4 \times 10^{-5}$
(Average density $=\frac{50+5}{2}=27.5 \mathrm{~V}$
Use of density $=\frac{\operatorname{mass}}{\text { voume }}$
Condone use of their density and volume
$($ mass $=) 6.6 \times 10^{-4}(\mathrm{~kg}) \checkmark$ c.a.o

## Alternative:

Use of Volume $=$ Thickness $x$ area of cross-section $\checkmark$
Condone POT errors apart from final answer

$$
(V=) 8 \times 10^{-4} \times 0.03 \operatorname{Or}(V=) 2.4 \times 10^{-5}
$$

Use of density $=\frac{\operatorname{mans}}{\text { voume }} /($ mass $=) 1.2 \times 10^{-3}$ or $1.2 \times 10^{-4} \checkmark$
(Average mass $=) \frac{1.2 \times 10^{-2}+1.2 \times 10^{-4}}{2} \checkmark$
$=6.6 \times 10-4(\mathrm{~kg}) \checkmark$ c.a.o
Condone use of their density and volume ( $50 \mathrm{~kg} \mathrm{~m}^{-3}=1.2 \times 10^{-3}$ )
$\left(5 \mathrm{~kg} \mathrm{~m}^{-3}=1.2 \times 10^{-4}\right)$

## Alternative:

Condone POT errors apart from final answer
Attempts to determine the area under the graph:
Formula for area of a rectangle added to the formula for area of a triangle seen / formula for the area of trapezium seen $\checkmark$

$$
\begin{aligned}
& 5 \times 0.03+\frac{(50-5) \times 0.03}{2}=0.825\left(\mathrm{~kg} \mathrm{~m}^{-2}\right) \\
& \text { or } \frac{50+5}{2} \times 0.03=0.825\left(\mathrm{~kg} \mathrm{~m}^{-2}\right)
\end{aligned}
$$

Multiplies their area by $8 \times 10^{-4} \mathrm{~J}$
Mass $=6.6 \times 10^{-4}(\mathrm{~kg}) \checkmark$ c.a.o
(d) $\mathbf{Q}$ has a larger volume (for the same mass and KE) /
$\mathbf{Q}$ has a larger surface area (for the same mass and KE) $\checkmark$
$\mathbf{Q}$ will experience a greater resistive force (at any given speed) / $\mathbf{Q}$ will displace more matter per unit distance $\sqrt{ }$
$\mathbf{Q}$ will do more work per unit distance / $\mathbf{Q}$ will transfer more of its kinetic energy per unit distance / $\mathbf{Q}$ will experience a greater deceleration $\checkmark$

Must have $\mathbf{Q}$ will travel a shorter distance for all 3 marks.
4. (a) Evidence of distance travelled = area under graph $=1755+1440+1620=4815$ J Full marks can be credited for use of suvat.

Average speed $=$ total distance/time taken $=4815 / 240$
$=20.1 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$ (at least 3sf)
Which is less than (speed) limit, (and therefore the answer is No). $\checkmark$
Allow ecf for distance in MP2
Only award MP3 for incorrect speed if attempt made to calculate distance correctly e.g. area under graph OR a.e. in distance or speed

Alternative for MP2 and MP3
Calculation of distance travelled at speed limit $=5280 \mathrm{~m} \checkmark$
Which is greater than distance travelled (so no). $\checkmark$
Alternative for MP1 and MP2:
Total area $=80.25 \mathrm{~m} \mathrm{~s}^{-1} \mathrm{~min} \checkmark$
Time $=4 \mathrm{~min}$
Average $=20.1 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
(b) Using reaction time of $2.0 \mathrm{~s} \checkmark$

Use of distance $=$ speed $\times$ time $=62 \mathrm{~m}$.
62 m (would be appropriate). $\checkmark$
Award MP2 if 1.6 s (to give 50 m ) or 1.8 s (to give 56 m ) or 1.7 s (to give 53 m ) or average of two distances used
Allow 60 m.
(c) Use of $\mathrm{F}=\mathrm{ma}$ to calculate acceleration.
$a=6800 / 1200 \checkmark=5.7 \mathrm{~m} \mathrm{~s}^{-2}$
evidence of use of suvat to calculate s or $\mathrm{t}, \boldsymbol{\downarrow}$
to give $t=5.5 \mathrm{~s} \checkmark$
$s=85 \mathrm{~m} . \checkmark$
If no other mark given, allow 1 mark for
$m v=1200 \times 31$ (= 37200)
Alternative for MP1 and MP2
$t=\frac{m v-m u}{F}$
Allow ce for a.
Allow ce for either incorrects or $t$.
(d) (It is assumed that) the car in front would take the same time/travel the same distance as the car behind when braking/ only difference is reaction time of the driver of car behind. $\checkmark$ Or
Car in front cannot stop instantaneously (so car behind will have time/distance to bring car to rest).or words to that effect

Alternative:
suggestion that total stopping distance is too large (drivers would ignore it/inefficient use of motorway)
(e) Correct use of cos (5) $\checkmark$
E.g.
$m g=N \cos (5)$
Correct use of $\sin (5) \checkmark$
E.g.
$N \sin (5)\left(=m v^{2} / r\right)$
So
$m v^{2} / r$ seen $\checkmark$
And $v=(r g \tan (5))^{1 / 2}$
Gives $v=(200 \times 9.81 \times \tan (5))^{1 / 2}=13$
So speed limit $=13 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
May see cos (85) for sin (5)
Alternative for MP1 and MP2: Evidence of mg tan (5)
fourth mark is for answer and suggesting this as the speed limit.
Max 3 if $m g=N$ used

