

## Superposition and Stationary Waves

Question Paper

Time available: 89 minutes Marks available: 65 marks

1. Figure 1 shows the apparatus a student uses to investigate stationary waves in a stretched string.

Two small pieces of adhesive tape are fixed to the string as markers $\mathbf{P}$ and $\mathbf{Q}$. Markers $\mathbf{P}$ and $\mathbf{Q}$ are 0.55 m apart and an equal distance from the ends of the string. A graph paper grid is placed behind the string between $\mathbf{P}$ and $\mathbf{Q}$.

Figure 1

not to scale
(a) The string is made to vibrate at the second harmonic.

Compare the motion of $\mathbf{P}$ with that of $\mathbf{Q}$.
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(b) The frequency of the vibration generator is increased, and a higher harmonic of the stationary wave is formed.

Figure 2 shows the string between $\mathbf{P}$ and $\mathbf{Q}$ at an instant in time. The dashed horizontal line indicates the position of the string at rest when the vibration generator is switched off.

Figure 2


The frequency of the vibration generator is 250 Hz .
Calculate the wave speed.
wave speed $=$ $\qquad$ $\mathrm{m} \mathrm{s}^{-1}$
(c) The instantaneous position of the string in Figure 2 can be explained by the superposition of two waves. The instantaneous positions of these waves between $\mathbf{P}$ and $\mathbf{Q}$ are shown in Figure 3.

Figure 3


Describe the properties that the waves must have to form the shape shown in Figure 2.
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(d) Figure $\mathbf{4}$ shows the positions of the two waves between $\mathbf{P}$ and $\mathbf{Q}$ a short time later.

Figure 4


Draw, on Figure 5, the appearance of the string between $\mathbf{P}$ and $\mathbf{Q}$ at this instant.
Figure 5

(e) Annotate (with an $\mathbf{A}$ ) the positions of any antinodes on your drawing in Figure 5.
(f) The frequency of the vibration generator is reduced until the first harmonic is observed in the string, as shown in Figure 6.

Figure 6


The string in Figure 6 is replaced with one that has 9 times the mass per unit length of the original string. All other conditions are kept constant, including the frequency of the vibration generator and the tension in the string.

Deduce the harmonic observed.
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2. Figure 1 shows a structure that supports a horizontal copper aerial wire $\mathbf{W}$ used for transmitting radio signals.

Figure 1


The copper aerial wire is 12 m long and its area of cross-section is $1.6 \times 10^{-5} \mathrm{~m}^{2}$.
The tension in the copper aerial wire is $5.0 \times 10^{2} \mathrm{~N}$.
Young modulus of copper $=1.2 \times 10^{11} \mathrm{~Pa}$
(a) Show that the extension produced in a 12 m length of the aerial wire when the tension is $5.0 \times 10^{2} \mathrm{~N}$ is less than 4 mm .
(b) The cables that support each mast are at an angle of $65^{\circ}$ to the horizontal.

Calculate the tension in each supporting cable so that there is no resultant horizontal force on either mast.

$$
\text { tension }=
$$

$\qquad$ N
(c) When wind blows, stationary waves can be formed on the aerial wire.

Explain how stationary waves are produced and why only waves of specific frequencies can form on the aerial wire.
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(d) Calculate the mass of a 1.0 m length of the aerial wire.

Density of copper $=8900 \mathrm{~kg} \mathrm{~m}^{-3}$
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mass = kg
(e) Calculate the frequency of the wave when the third harmonic is formed on the aerial wire.
frequency =
$\qquad$ Hz
(f) Sketch, on Figure 2, the standing wave on the wire when the third harmonic is formed.

Figure 2

(g) High winds produce large amplitudes of vibration of the aerial wire.

Explain why the wire may sag when the high wind stops.
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3. This question is about an experiment to measure the wavelength of microwaves.

A microwave transmitter $\mathbf{T}$ and a receiver $\mathbf{R}$ are arranged on a line marked on the bench.
A metal sheet $\mathbf{M}$ is placed on the marked line perpendicular to the bench surface.
Figure 1 shows side and plan views of the arrangement.
The circuit connected to $\mathbf{T}$ and the ammeter connected to $\mathbf{R}$ are only shown in the plan view.
Figure 1
side view


The distance $y$ between $\mathbf{T}$ and $\mathbf{R}$ is recorded.
$\mathbf{T}$ is switched on and the output from $\mathbf{T}$ is adjusted so a reading is produced on the ammeter as shown in Figure 2.

Figure 2

$\mathbf{M}$ is kept parallel to the marked line and moved slowly away as shown in Figure 3.
Figure 3


The reading decreases to a minimum reading which is not zero.
The perpendicular distance $x$ between the marked line and $\mathbf{M}$ is recorded.
(a) The ammeter reading depends on the superposition of waves travelling directly to $\mathbf{R}$ and other waves that reach $\mathbf{R}$ after reflection from $\mathbf{M}$.

State the phase difference between the sets of waves superposing at $\mathbf{R}$ when the ammeter reading is a minimum.
Give a suitable unit with your answer.
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(b) Explain why the minimum reading is not zero when the distance x is measured.
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(c) When $\mathbf{M}$ is moved further away the reading increases to a maximum then decreases to a minimum.

At the first minimum position, a student labels the minimum $n=1$ and records the value of $x$.
The next minimum position is labelled $n=2$ and the new value of $x$ is recorded.
Several positions of maxima and minima are produced.
Describe a procedure that the student could use to make sure that $\mathbf{M}$ is parallel to the marked line before measuring each value of $x$.
You may wish to include a sketch with your answer.
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(d) It can be shown that

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n=\sqrt{4 x^{2}+y^{2}}-y
$$

where $\lambda$ is the wavelength of the microwaves and $y$ is the distance defined in Figure 1.
The student plots the graph shown in Figure 4.
The student estimates the uncertainty in each value of $\sqrt{4 x^{2}+y^{2}}$ to be 0.025 m and adds error bars to the graph.

Determine

- the maximum gradient $G_{\max }$ of a line that passes through all the error bars
- the minimum gradient $G_{\min }$ of a line that passes through all the error bars.

$$
\begin{aligned}
& G_{\max }= \\
& G_{\min }=
\end{aligned}
$$

(e) Determine $\lambda$ using your results for $G_{\text {max }}$ and $G_{\text {min }}$.

$$
\lambda=\ldots \mathrm{m}
$$

Figure 4

(f) Determine the percentage uncertainty in your result for $\lambda$.
(g) Explain how the graph in Figure 4 can be used to obtain the value of $y$. You are not required to determine $y$.
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(h) Suppose that the data for $n=13$ had not been plotted on Figure 4.

Add a tick $(\checkmark)$ in each row of the table to identify the effect, if any, on the results you would obtain for $G_{\max }, G_{\text {min }}, \lambda$ and $y$.

| Result | Reduced | Not affected | increased |
| :---: | :---: | :---: | :---: |
| $G_{\max }$ |  |  |  |
| $G_{\min }$ |  |  |  |
| $\lambda$ |  |  |  |
| $y$ |  |  |  |

4. Figure 1 and Figure 2 show a version of Quincke's tube, which is used to demonstrate interference of sound waves.

Figure 1


Figure 2


A loudspeaker at $\mathbf{X}$ produces sound waves of one frequency. The sound waves enter the tube and the sound energy is divided equally before travelling along the fixed and movable tubes. The two waves superpose and are detected by a microphone at $\mathbf{Y}$.
(a) The movable tube is adjusted so that $d_{1}=d_{2}$ and the waves travel the same distance from $\mathbf{X}$ to $\mathbf{Y}$, as shown in Figure 1. As the movable tube is slowly pulled out as shown in Figure 2, the sound detected at $\mathbf{Y}$ gets quieter and then louder.

Explain the variation in the loudness of the sound at $\mathbf{Y}$ as the movable tube is slowly pulled out.
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(b) The tube starts in the position shown in Figure 1.

Calculate the minimum distance moved by the movable tube for the sound detected at $\mathbf{Y}$ to be at its quietest.
frequency of sound from loud speaker $=800 \mathrm{~Hz}$
speed of sound in air $=340 \mathrm{~m} \mathrm{~s}^{-1}$
minimum distance moved $=$ $\qquad$ m
(c) Quincke's tube can be used to determine the speed of sound.

State and explain the measurements you would make to obtain a value for the speed of sound using Quincke's tube and a sound source of known frequency.
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5. Figure 1 is a diagram of a microwave oven.

Figure 1


A student wants to use the stationary waves formed in the microwave oven to measure the frequency of the microwaves emitted by the transmitter.
(a) Suggest how stationary waves are formed in the microwave oven.
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(b) The student removes the turntable and places a bar of chocolate on the floor of the oven. He then switches the oven on for about one minute. When the chocolate is removed the student observes that there are three small patches of melted chocolate with unmelted chocolate between them. Figure $\mathbf{2}$ is a full-sized diagram of the chocolate bar.

Figure 2


Suggest why the chocolate only melts in the positions shown.
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(c) Calculate, by making suitable measurements on Figure 2, the frequency of the microwaves used by the oven.

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\text { frequency }=\ldots \mathrm{Hz}
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(d) Explain why most microwave ovens contain a rotating turntable on which the food is placed during cooking.
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