

A-Level Physics

The Young Modulus

Mark Scheme

Time available: 66 minutes Marks available: 46 marks

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Mark schemes

1.

(a) place mirror behind ruler $_1\checkmark$

adjust position (of eye / head) until pin hides its own reflection $_2\checkmark$

for $\sqrt{1}$ do not insist on contact between mirror and ruler; accept sketch if mirror is parallel to ruler for $\sqrt{2}$ accept (pin lines up with reflection (image))

for $_2 \checkmark$ accept 'pin lines up with reflection / image'

allow $_{12}\checkmark = 1 MAX$

for convincing explanation of set-square placed against vertical ruler then aligned with pin

OR

move (clamped) ruler closer to pin

2

(b) strategy:

y (as the dependent variable) <u>measured</u> for different values of one independent variable ${}_1 \checkmark$

identifies <u>one</u> correct control variable $_2\checkmark$

for $_{1}\sqrt{accept y read OR <u>recorded</u>;}$

for $_2\checkmark$ control variables *m* OR *L* only;

m = independent variable and L = control variable OR

 $m = \text{control variable and } L = \text{independent variable}_{12} \checkmark \checkmark$

if *L* is being varied and m = 250 g is stated, this can be taken as m = control variable and therefore known;

take a similar approach if m is being varied but in this case L must be <u>less than</u> 30 cm

idea that w and/or t are control variables is neutral

for more than one independent variable, eg variation of both *m* and $L_{12}XX$ but allow ecf for $_{4}\checkmark$ as long as plot is valid, eg y against mL^{3}

2

1

suitable measuring instruments for *L*, *w* and $t_{3}\checkmark$

use of ruler to measure *L* AND use of micrometer screw gauge OR <u>digital</u> / electronic callipers to obtain w <u>and</u> *d* procedures to reduce random / systematic error are neutral

analysis:

2.

suggests valid plot ₄√

identifies correctly how E can be found ${}_5\checkmark$

for $_{4}\checkmark$ expect *y* [by itself or combined with another factor] on the vertical axis and their independent variable / some <u>valid</u> <u>manipulation</u> of their independent variable on the horizontal axis for $_{5}\checkmark E$ must be the subject of the expression given examples:

plot y against m $4\checkmark E = \frac{4 \times L^3 \times g}{w \times t^3 \times \text{gradient}} 5\checkmark$ plot y against $L^3 4\checkmark E = \frac{4 \times m \times g}{w \times d^3 \times \text{gradient}} 5\checkmark$ plot y against $\frac{4 \times L^3}{w \times t^3} 4\checkmark E = \frac{m \times g}{\text{gradient}} 5\checkmark$ log y against log m $4\checkmark E = \frac{4 \times g \times L^3}{w \times t^3 \times 10^{\text{intercept}}} 5\checkmark$ log y against log L $4\checkmark E = \frac{4 \times m \times g}{w \times t^3 \times 10^{\text{intercept}}} 5\checkmark$

[7]

2

(a) correctly deduces extension is 2.6 or 2.7 mm \checkmark

Should see $AC^2 = 1.50^2 + (6.34 \times 10^{-2})^2$; (new) AC = 1.50134; Extension of AC = (1.50134 - 1.50 =) 0.00134 m or 1.34 mm; and then doubles this Final value must be to at least 2 sf

(b) evidence of correct working: ✓

$$\sin \theta = \frac{6.34 \times 10^{-2}}{\text{their new AC}} \quad \text{or } \theta = 2.42^{\circ} \text{ seen}$$

OR

 $W = 2T \sin \theta$ seen

OR

suitable vector diagram with θ labelled

tension correctly calculated from $\frac{1.0}{2 \times \text{their sin}\theta} \checkmark$ For $_1 \checkmark$ acceptable diagrams are shown below

Correct final answer of 11.8 N or 12 N earns both marks

(C) ruled best-fit line between first and sixth points;

line must pass above 2nd point

and

(a)

(b)

3.

must pass below 4th point ₁√ for $\sqrt{1}$ withhold mark if line is thick, faint or discontinuous gradient calculated from $\frac{\Delta(W/y)}{\Delta y^2}$ with $\Delta y^2 \ge 0.004_2$ (gradient ~ 3850) for $_{2}\sqrt{}$ condone read off errors of ± 1 division for $_{3}\checkmark$ note that $1.50^{3} = 3.375$ so allow sub of 3.38 for $_{4}\checkmark$ reject 2 sf 1.2 x 10¹¹ evidence of using E = $\frac{\text{their gradient} \times 1.50^3}{1.11 \times 10^{-7}} \sqrt{34}$ for $_{3}\checkmark$ note that $1.50^{3} = 3.375$ so allow sub of 3.38 *E* in range 1.10 \times 10¹¹ to 1.24 \times 10¹¹ (Pa) ₄ \checkmark for $_{4}\sqrt{reject 2}$ sf 1.2 $\times 10^{11}$ (d) kg s⁻² \checkmark no credit for N m⁻¹ correct answer only Attempt to resolve **A** or **B** eg 430 × cos35° or $T_{\rm B}$ × cos12° \checkmark 360 (N) 🗸 If no other mark given, allow $430 \times \sin 35^\circ = T_B \times \sin 12^\circ$ to give 1190 N for 1 mark. Substitution of F and A into Young modulus or stress equation \checkmark 4.4 × 10⁻² (m) √ Condone POT error for Young modulus

2

2

4

1

[8]

(c) Angle of **A** decreases or angle of **B** increases \checkmark

Accept references to 35° or 12°

Any correct application of trig or geometry to the situation

(eg $T_B/T_A = \cos\theta_A/\cos\theta_B$ so as θ_A decreases, $\cos\theta_A$ increases, $\cos\theta_B$ decreases, so T_B/T_A increases)

OR

eventually $\theta_{\rm B}$ will equal 35°, $\theta_{\rm A}$ = 12° so forces will be reversed (as system is symmetrical)

OR

sum of vertical components remains unchanged and vertical component of tension becomes less as angle ${\bf A}$ decreases \checkmark

Allow idea that more of the weight is supported by **B**

 T_A decreases, following some relevant discussion \checkmark

3

(d) Greater rate occurs when pulses are shorter (in time)/less modal dispersion ✓ Allow reverse arguments

Smaller diameter (leads to less modal dispersion) means smaller range of path lengths ✓ Accept idea of fewer reflections

X is more suitable because narrower core leads to lower modal dispersion or reduced pulse broadening \checkmark

[10]

3

1

1

4.

(a) 37.8 **√**

CAO

(b) random (error)

condone 'statistical' 🗸

the following are neutral: 'parallax' / 'human (error)' / '(some) results are anomalous' (c) advantage (of using thinner beam):

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(same load produces) larger (values of) s or wtte 1\checkmark
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SO

the <u>percentage</u> uncertainty / error (in s) is reduced $2\sqrt{}$

for 1√ accept 'beam bends / deflects more' 'beam extends more' / 'easier to bend' are neutral for 2√ the following are neutral: 'easier to make readings' / 'values (of s) are more accurate' / 'more precise' / 'less mass needed' / 'wider range of readings'

disadvantage (of beam bending more):

idea that beam may undergo plastic deformation 3

so

the graph will be non-linear / curve or wtte 4√

or

beam 'may break' / 'slip off knife edges' **and** relevant comment about safety / health / hazard / 'cannot get unload data'

or

reduces range of *m* or wtte **and** relevant comment about the effect on the graph, eg increase scatter $34\sqrt{} = 1 \text{ MAX}$

for 3 ✓ accept / 'beam may become permanently deformed' or wtte / 'necking may occur' / 'hysteresis may occur' / 'beam can reach (go past) elastic limit' the following are neutral: 'causes systematic error' / 'beam may go past limit of

proportionality' / 'need to increase height of supports' / 'beam may bend under own weight'

MAX 3

(d) $E \approx 10^9$

or

1.14 × 10⁹ seen 1√

for $1\checkmark$ accept 10^9 seen in working

1

correct manipulation seen in **body of answer** of $s = \frac{\eta m}{E} 2^{\checkmark}$

for 2√ either

substitution of their *E* and data from **Figure 8** leaving η as only unknown: allow POT in *s* but not in *m*

eg
$$\eta = \frac{\text{their } E \times 25.5 \left(\times 10^{-3} \right)}{0.25}$$
 or

substitution of their *E* and result of a gradient calculation: allow POT in Δs but not in Δm

$$eg \eta = 1.14 \times 10^9 \times 1.02 (\times 10^{-1}) \text{ or }$$

calculation involving orders of magnitude (expect 10^{-1} but allow 10^{2} for gradient)

$$eg \eta \approx 10^9 \times 10^{-1}$$

2

correct raw result (allow POT in *E*) $3\checkmark$

for $3\checkmark$ expect 1.16 × 10⁸ but allow 1 sf gradient eg leading to 1.14 × 10⁸

(on answer line) order of magnitude consistent with their raw result 4

for $4\checkmark \eta = 10^8$ or 8 only; allow use of their *E* award $34\checkmark = 1$ MAX for use of gradient ≈ 100 leading to order of magnitude = 10^{11} or 11 only

-		
-		
-		

(e) identifies that s and L are linked by a power law \checkmark

accept any correct expression (unless there is talk-out) with s or log s as the subject; treat any quantities other than s and L as constant except E and η possible answers are: $s \propto L^n$ allow $s \propto L^m$ if m identified as constant $s \propto L^3$ $s = kL^n$ $\log s = n \log L + (\log) k$ $\log s = 3 \log L + (\log) k$ $\log s = \log L^3 + (\log) k$ reject $s = L^n$ $\log s = n \log L$ $\log s \propto n \log L$ $10^{\rm s} \propto 10^{\rm L}$'s and L are linked logarithmically' 's is directly proportional to L'

(f)
$$(\log L =) -0.097$$
 seen

for $1\checkmark$ accept any log L rounding to -0.097;

or

working on Figure 5 confirming a value of log L between -0.095 and -0.100 1 \checkmark

uses **Figure 5** to obtain *s* in range 2.9 to 3.1×10^{-2} (m) $2\checkmark$ working can be suitable ruled line or mark on the best-fit line / on graph axes for $2\checkmark$ accept 29, 30 or 31 mm etc reject 1sf 3×10^{-2} (m)

use of wrong base

 $\ln L = -0.22(3);$

uses **Figure 5** to obtain *s* in range 1.49 to 1.51×10^{-1} or 1.5×10^{-1} (m) $12\sqrt{accept \ 15 \ cm \ etc}$

1

1

1

use of **Figure 4** to determine $M \checkmark$ (g) their (final answer to) (f) \times gradient of Figure 4 (9.8 \pm 2.5%) minimum 2sf condone use of 1sf s 1 [13] Sum of / total clockwise moments = sum of / total anticlockwise moments√ (a) 5. For a body in equilibrium√ 2 Clockwise moments = 2.0 × 9.81 × 0.25 + 0.65 × 9.81 × 0.45 (b) = 7.77 (N m)√ Anticlockwise moments = $Tsin30 \times 0.3\sqrt{}$ Tsin30 × 0.3 = 7.77 or T = 7.77/(sin30 × 0.3) ✓ T = 52.0 (N) ✓ First mark for clockwise moments, workings or correct answer. Second mark for anticlockwise moments. Third mark for equating clockwise and anticlockwise moments. Fourth mark for correct answer. 4 tensile stress = $52.0/(7.8 \times 10^{-7}) = 6.6 \times 10^7 \checkmark$ (C) tensile strain = $6.6 \times 10^7 / (180 \times 10^9) = 3.7 \times 10^{-4} \checkmark$

2

[8]