

# A-Level Physics 

## The Young Modulus

## Question Paper

Time available: 66 minutes Marks available: 46 marks

1. Figure 1 shows a strip of steel of rectangular cross-section clamped at one end. The strip extends horizontally over the edge of a bench.

Figure 1

end view of unloaded steel strip

(a) A mass $m$ is suspended from the free end of the strip.

This produces a vertical displacement $y$.
A student intends to measure $y$ with the aid of a horizontal pin fixed to the free end of the steel strip.
She positions a clamped vertical ruler behind the pin, as shown in Figure 2.
Figure 2
plan view


Explain a procedure to avoid parallax error when judging the reading indicated by the position of the pin on the ruler.
You may add detail to Figure 2 to illustrate your answer.
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$\qquad$
(b) It can be shown that

$$
y=\frac{4 m g L^{3}}{E w t^{3}}
$$

where:
$L$ is the distance between the free end of the unloaded strip and the blocks $w$ is the width of the strip and is approximately 1 cm
$t$ is the thickness of the strip and is approximately 1 mm
$E$ is the Young modulus of the steel.
A student is asked to determine $E$ using the arrangement shown in Figure 1 with the following restrictions:

- only one steel strip of approximate length 30 cm is available
- $\quad m$ must be made using a 50 g mass hanger and up to four additional 50 g slotted masses
- the experimental procedure must involve only one independent variable
- a graphical method must be used to get the result for $E$.

Explain what the student must do to determine $E$.
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2. A student does an experiment to determine the Young modulus of a metal.

Figure 1 shows a wire made from the metal clamped at points $\mathbf{A}$ and $\mathbf{B}$ so that the wire is horizontal. The horizontal distance between $\mathbf{A}$ and $\mathbf{B}=3.00 \mathrm{~m}$.
$\mathbf{C}$ is the mid-point on the wire between $\mathbf{A}$ and $\mathbf{B}$.
Figure 1


A mass of weight $W$ is suspended at $\mathbf{C}$ to extend the wire. Figure $\mathbf{2}$ shows that $\mathbf{C}$ moves vertically downwards by a distance $y$.

Figure 2

(a) When $W$ is $1.0 \mathrm{~N}, y$ is 6.34 cm .

Show that the wire extends by approximately 3 mm .
(b) Calculate the tension in the wire when $W$ is 1.0 N .

$$
\text { tension }=\ldots \mathrm{N}
$$

It can be shown that

$$
\frac{W}{y}=\frac{E A y^{2}}{x^{3}}+k
$$

$$
\text { where } \quad \begin{aligned}
E & =\text { Young modulus of the metal } \\
A & =1.11 \times 10^{-7} \mathrm{~m}^{2} \\
x & =1.50 \mathrm{~m} \\
k & =\text { a constant } .
\end{aligned}
$$

A student measures $y$ for different values of $W$ and plots the graph shown in Figure 3.
Figure 3

(c) Determine $E$ using Figure 3.

$$
E=\ldots \mathrm{Pa}
$$

(d) Deduce the fundamental base units for $k$.
fundamental base units for $k=$ $\qquad$
3. The diagram shows a camera filming a sports event from above. The position of the camera is controlled by two steel cables, A and B, that pass over fixed, smooth pulleys.

(a) In the diagram above the camera is stationary. The tension in $\mathbf{A}$ is 430 N and $\mathbf{A}$ makes an angle of $35^{\circ}$ to the horizontal. B makes an angle of $12^{\circ}$ to the horizontal.

Calculate the tension in $\mathbf{B}$.
$\qquad$ N
(b) The cross-sectional area of $\mathbf{A}$ is $7.0 \times 10^{-6} \mathrm{~m}^{2}$. The unstretched length of $\mathbf{A}$ is 150 m .

Calculate the extension of $\mathbf{A}$ when the tension in it is 430 N .
Young modulus of steel $=210 \mathrm{GPa}$
extension =__m
(c) The camera is moved horizontally to the right to a new stationary position. The tension in $\mathbf{A}$ is now different from that in the diagram above.

Deduce whether the tension in $\mathbf{A}$ has increased or decreased.
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$\qquad$
(d) The camera's signal is transmitted as a series of pulses through an optical fibre. The table shows data for two optical fibres $\mathbf{X}$ and $\mathbf{Y}$. Both optical fibres are identical except for their core diameter.

| Optical fibre | Core diameter / $\mu \mathrm{m}$ |
| :---: | :---: |
| $\mathbf{X}$ | 8 |
| $\mathbf{Y}$ | 50 |

Deduce which fibre allows a greater pulse transmission rate.
$\qquad$
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$\qquad$
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(Total 10 marks)
4. Figure 1 shows apparatus used to investigate the bending of a beam.

Figure 1


The beam is placed horizontally on rigid supports.
The distance $L$ between the supports is 80 cm .
A travelling microscope is positioned above the midpoint of the beam and focused on the upper surface.
(a) Figure 2 shows an enlarged view of both parts of the vernier scale.

Figure 2


The smallest division on the fixed part of the scale is 1 mm .
What is the value of the vernier reading $R_{0}$ in mm ?
Tick ( $\checkmark$ ) one box.
34.8

37.8

45.8

49.8

(b) Figure 3 shows the beam bending when a hanger of mass 0.050 kg is suspended from the midpoint.

Figure 3


The microscope is refocused on the upper surface and the new vernier reading $R$ is recorded.
The vertical deflection $s$ of the beam is equal to $\left(R-R_{0}\right)$.
The total mass $m$ suspended from the beam is increased in steps of 0.050 kg .
A value of $s$ is recorded for each $m$ up to a value of $m=0.450 \mathrm{~kg}$.
Further values of $s$ are then recorded as $m$ is decreased in 0.050 kg steps until $m$ is zero.
Student A performs the experiment and observes that values of $s$ during unloading are sometimes different from the corresponding values for loading.

State the type of error that causes the differences student $\mathbf{A}$ observes.
$\qquad$
(c) Student B performs the experiment using a thinner beam but with the same width and made from the same material as before.

Discuss one possible advantage and one possible disadvantage of using the thinner beam.

Advantage $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Disadvantage $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(d) Figure 4 shows the best-fit line produced using the data collected by student $\mathbf{A}$.

Figure 4


It can be shown that $s=\frac{\eta m}{E}$
where $E$ is the Young modulus of the material of the beam and $\eta$ is a constant.
Deduce in $\mathrm{s}^{-2}$ the order of magnitude of $\eta$.

$$
E=1.14 \mathrm{GPa}
$$

$\qquad$ $\mathrm{s}^{-2}$
(e) Student $\mathbf{C}$ performs a different experiment using the same apparatus shown in Figure 1. A mass $M$ is suspended from the midpoint of the beam.
The vertical deflection $s$ of the beam is measured for different values of $L$.
Figure 5 shows a graph of the results for this experiment.
Figure 5


Figure 5 shows that $\log 10(s / m)$ varies linearly with $\log 10(L / m)$.
State what this shows about the mathematical relationship between $s$ and $L$. You do not need to do a calculation.
$\qquad$
$\qquad$
$\qquad$
(f) Deduce, using Figure 5, the value of $s$ when $L=80 \mathrm{~cm}$.

$$
s=\ldots \mathrm{m}
$$

(g) Determine $M$ using Figure 4.

$$
M=
$$

$\qquad$ kg
5. The diagram below shows a vase placed on a uniform shelf that is supported by a steel wire.


The mass of the vase is 0.65 kg and the mass of the shelf is 2.0 kg . The shelf is hinged at A . The steel wire is attached to the shelf 0.30 m from A and is at an angle of $30^{\circ}$ to the shelf. The other end of the steel wire is attached to the wall.
(a) State the principle of moments.
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$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) Show, by taking moments about A, that the tension in the steel wire is about 50 N .
(c) The cross-sectional area of the steel wire is $7.8 \times 10^{-7} \mathrm{~m}^{2}$. The steel has a Young modulus of 180 GPa .

Calculate the tensile strain of the steel wire when it is holding up the shelf and the vase.
tensile strain =

