# 

## GCSE Mathematics

8300/1H-Paper 1 Higher Tier Mark scheme

8300

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Version/Stage: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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### **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
A	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
М dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a ≤ value < b
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

#### Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

#### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

#### Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

#### Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

#### Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

#### Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

#### Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

#### **Continental notation**

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Question	Answer	Mark	Commer	its
1	40	B1		
2	$\begin{pmatrix} 2 \\ -3 \end{pmatrix}$	B1		
3	$5a - 4a^2$	B1		
4	500	B1		
5	5x + 15 < 60 or 5x < 45 or x + 3 < 12 x < 9 or 9 > x	M1 A1	SC1 incorrect sign eg $x \le 9$ or $x = 9$ or $x = 3$ or $x = < 9$ or answer of	> 9 or <i>x</i> ≥ 9 9
	Additional Guidance			
	Allow use of other inequality signs or = if recovered to answer of $x < 9$ M1.			M1A1
	Embedded answer of 5(9 + 3) < 60M0A0			M0A0
	5x + 3 < 60 followed by $x + 3 < 12$ followed by $x < 9is not a recovery, but is two errors M0A0$			MOAO

Question	Answer	Mark	Comments	
	<u>1.86</u> 1.6(0)	M1	oe $\frac{0.93}{0.8(0)}$ or $1\frac{0.26}{1.6}$	
	<u>186</u> 160 or 1 <u>26</u> 160	oe with no decimal value	25	
	<u>93</u> 80 or 1 <u>13</u> 80	D1#	ft correct simplification of using the digits 186 and	f their fraction 16(0)
		ΒΊΠ	ignore incorrect conversi mixed number	on from $\frac{93}{80}$ to a
	Add	litional G	uidance	
	Cannot score B1ft from an incorrect m	ixed num	per	
	$\frac{160}{186} = \frac{80}{93}$			M0A0B1ft
	6 $\frac{\frac{80}{93}}{\frac{93}{80}} = 1 \frac{3}{\frac{80}{80}}$ (incorrect conversion to mixed number)			
6				
	$\frac{186}{160} = \frac{31}{30}$ (incorrect simplification of fraction)			M1A1B0
	$\frac{93}{80} = \frac{31}{30}$ (incorrect simplification of fraction)			
	$\frac{93}{80} = \frac{0.93}{0.8}$ (incorrect simplification of fraction)		M1A1B0	
	$\frac{186}{16} = \frac{93}{8}$			M0A0B1ft
	$\frac{1.86}{1.6} = \frac{9.3}{8}$ M1			
	$\frac{1.86}{1.6} = \frac{186}{16} = \frac{93}{8}$			M1A0B1ft
	$\frac{1.86}{1.6} = \frac{86}{60} = \frac{43}{30}$ (simplification does	not come	from 186 and 16(0))	M1A0B0

Question	Answer	Mark	Commer	nts
7	<i>x</i> -coordinate of $C = 12$ or <i>y</i> -coordinate of $C = 8$ or 12 marked on <i>x</i> -axis below <i>C</i> and 8 marked on <i>y</i> -axis left of <i>C</i> or <i>x</i> -coordinate of $D = 6 + 6 + 6$ or <i>y</i> -coordinate of $D = 2 + 3 + 3 + 3$ or $\frac{x}{6} = 3$ or $6 = (2 \times 0 + x) \div 3$ or $\frac{y-2}{5-2} = 3$ or $5 = (2 \times 2 + y) \div 3$ or 18 marked on <i>x</i> -axis below <i>D</i> or 11 marked on <i>y</i> -axis left of <i>D</i> ( <i>C</i> is the point) (12, 8) or ( <i>D</i> is the point) (18,) or (, 11) or 18 marked on <i>x</i> -axis below <i>D</i>	M1 A1	oe sets up a correct equati <i>x</i> -coordinate of <i>D</i> or <i>y</i> -c condone missing brack clear	on for oordinate of <i>D</i> ets if intention is
	18 11	Δ1		
	Add	litional G	uidance	
	(12,8 , 18,11) on answer line with prev (12,8 , 18,11) on answer line with no p	rious link t previous lin	o C and D nk to C and D	M1A1A1 M1A1A0
	12, 8 on answer line with no other wo	rking		M1A1A0
	Accept correct working on diagram an not contradicted by answer line	d correct a	answer on diagram if	
	11, 18 on answer line does not score t M1A0 or M1A1	he last m	ark, but may score	
	11, 18 with no working			M0A0A0

Question	Answer	Mark	Commer	nts
			-	
	$\frac{31}{50}$ or 0.62 or 62%	B1	oe fraction, decimal or p	ercentage
	Ado	litional G	uidance	
	31 or 62			B0
	31 : 50	B0		
8(a)	31 out of 50 or 31 in 50	B0		
	Ignore subsequent attempts to simplify	$\frac{31}{50}$ or c	onvert it to a decimal or	
	percentage, eg $\frac{31}{50} = 0.6$			
	$\frac{31}{50} = 0.5$ oe is considered as choice			BO

Question	Answer	Mark	Commer	nts
	Valid reason	B1ft	eg 31 is more than 19 (12) more heads than tai 31 is more than 25 31 $\neq$ 25 (6) more than expected it should be 25 times heads and tails should b it landed on heads more times relative frequency/probal than 0.5 ft if their 0. 0.62 > 0.5 ft if their 0.	ls e (roughly) equal than half the bility is more 62 > 0.5 62 > 0.5
	Add	litional G	uidance	
	ft is only available if comparing their re relative frequency must be greater tha			
8(b)	b) Condone the probability given as 50/50 in otherwise correct reasons eg Probability is 50/50 so there should be 25 heads			
	There were only 19 tails	B1		
	There weren't enough tails			B1
	Because it landed on heads 31 times a	and it sho	uld be 25/25	B1
	It should be $\frac{1}{2}$			B1
	The probability should be $\frac{1}{2}$ but it land	ds on head	ds 31 times	B1
	There were 31 heads			B0
	There were 19 tails			B0
	There were 31 heads and 19 tails			B0
	The coin could be fixed			B0
	Incorrect statement eg 31 is 22 more	than 19		B0

Question	Answer	Mark	Comme	ents
	Alternative method 1			
	$-2\frac{7}{8} + 15\frac{1}{4}$ or $15\frac{2}{8}$ or (-)2.875 and 15.25 or (-) $\frac{23}{8}$ and $\frac{61}{4}$	M1	oe common denominator fo parts of the mixed numb conversion of both numb with at least one correct conversion of both numb fractions with at least on	or both fractional ers pers to decimals pers to improper e correct
	$-2\frac{7}{8} + 15\frac{2}{8}$ or -2.875 + 15.25 or $-\frac{23}{8} + \frac{122}{8}$	M1dep	oe common denominato correct decimals oe common denominato	r
	$\frac{99}{8}$ or $12\frac{3}{8}$ or 12.375	A1	oe fraction, mixed numb	er or decimal
	Alternative method 2			
9	$-2 + 15 \text{ and } (-)\frac{7}{8} + \frac{1}{4}$ M1 $-2 + 15 \text{ and } (-)\frac{7}{8} + \frac{2}{8}$ M1dep or $13 - \frac{5}{8}$	M1		
		oe common denominato	r	
	$\frac{99}{8}$ or 12 $\frac{3}{8}$ or 12.375	A1	oe fraction, mixed numb	er or decimal
	Additional Guidance			
	$15\frac{1}{4} - 2\frac{7}{8}$ scores M0, but followed	by $15\frac{2}{8}$ + 2	2 <sup>7</sup> _scores M1 on Alt 1 8	
	Values in 2 <sup>nd</sup> mark must be correct; no	ft from inc	correct conversion	
	$\frac{99}{8}$ incorrectly converted to a decimal or mixed number			M1M1A1
	13 <u>-5</u> 8			M1M1A0

Question	Answer	Mark	Comme	ents
10	(x =) 3 and (y =) 2 in correct positions	B2	B1 $y = \frac{24}{x}$ or $4 = \frac{k}{6}$ or $k$ or $(x =)$ 3 in correct poson or $(y =)$ 2 in correct poson	z = 24 oe ition above 8 ition below 12
	Ade	ditional G	uidance	
	$y = \frac{1}{kx}$ or $4 = \frac{1}{6k}$ oe followed by $k =$ in table	$\frac{1}{24}$ , with r	no or incorrect values	B1

Question	Answer	Mark	Comments		
	Alternative method 1 – width of sm	all rectar	igle is <i>x</i> (any letter)		
	x  and  2x  or  x + 2x + x + 2x  or  6x	M1	ое		
	x + 2x + x + 2x = 15 or $6x = 15$	M1dep	oe		
	(x =) 2.5	A1	from correct working or with 5 as the other dimension or with 7.5 as the length of the large rectangle		
	25	A1ft	ft 10 × their 2.5 with M1M1 awarded		
	Alternative method 2 – length of sn	nall recta	ngle is <i>x</i> (any letter)		
	$x \text{ and } \frac{x}{2} \text{ or } x + \frac{x}{2} + x + \frac{x}{2} \text{ or } 3x$	M1	oe		
11	$x + \frac{x}{2} + x + \frac{x}{2} = 15$	M1dep	oe		
	or $3x = 15$				
	(x =) 5	A1	from correct working or with 2.5 as the other dimension or with 7.5 as the length of the large rectangle		
	25	A1ft	ft 5 × their 5 with M1M1 awarded		
	Alternative method 3 –				
	a = width of small rectangle and $b$ =	= length c	of small rectangle (any letters)		
	b = 2a or 10 $a$ or 5 $b$	M1	correct expression for perimeter of the large rectangle in one variable		
	6a = 15 or 3b = 15	M1dep	correct equation in one variable		
	( <i>a</i> =) 2.5 or ( <i>b</i> =) 5	A1	from correct working or with both values correct or with one value correct and 7.5 as the length of the large rectangle		
	25	A1ft	ft 10 × their $a$ or 5 × their $b$ with M1M1 awarded		

	Alternative method 4 – trial and improvement using ratio of sides			
	length = $2 \times$ width seen or implied M1			
	Two correctly evaluated trials for perimeter of small rectangle with length = $2 \times \text{width}$	M1dep	eg 8 + 4 + 8 + 4 = 24 and 10 + 5 + 10 + 5 = 30	
	2.5 and 5	A1	implied by 2.5 + 5 + 2.5	+ 5 = 15
	25	A1		
11(cont)	Additional Guidance			
	Note that there is no ft in method 4         In all methods, marks can be awarded for annotation of the diagram, with lengths clearly identified, or working inside or alongside the diagram			
	eg 2.5 and 5 marked correctly as the	dimensior	ns of the small rectangle	M1M1A1
	2.5 marked as the width of the small rectangle and 7.5 marked as the length of the large rectangle M1M1A1			M1M1A1
	If full marks not awarded, mark both the diagram and working then award the better mark			
	In alt 4, one or more trials may be crossed out to indicate that they do not give the correct perimeter. Do not treat this as the usual crossed out work not to be marked if replaced.			

Question	Answer	Mark	C	omments
	One correct conversion to a comparable form $0.08 \times 10^{-2}$ or $0.0008$ $400 \times 10^{-4}$ or $0.04$ $0.06 \times 10^{-2}$ or $0.0006$ $7 \times 10^{-2}$ or $700 \times 10^{-4}$	M1		
	$6 \times 10^{-4}$ $8 \times 10^{-4}$ $4 \times 10^{-2}$ 0.07 with no clearly incorrect working	A1	oe accept in converte	ed form
Additional Guidance				
_	Correct answer from clearly incorrect working			A0
	Accept numbers with two decimal points if it is clear that the point has been moved to the correct place eg 0.0008.0 with curved lines between each place value between the decimal pointsIf the numbers are converted into fractions, at least two must be given correctly with common denominators to score the first mark eg $\frac{4}{100}$ and $\frac{7}{100}$			
-				
	eg $\frac{6}{1000}$ and $\frac{8}{1000}$ only			МО
	eg $\frac{6}{10000}$ and $\frac{7}{100}$ only			МО

13	15 000 mm <sup>3</sup>	B1	
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Question	Answer	Mark	Commer	nts
	At least 3 correct pairs from		0e pairs may be seen as rat	ios
	20 and 20		pairs may be seen as rai	.105
	25 and 24			
	30 and 28			
	35 and 32			
	40 and 36			
	or	M1		
	9(10+5n) = 10(12+4n)		oe equation, where <i>n</i> is the new rows (correct answe	ne number of
	or		new rows (conect answe	1 15 0)
	9(5n) = 10(4n + 4)		oe equation, where $n$ is the of rows (correct answer is	ne total number
14(a)	or			50)
	9(5+5n) = 10(8+4n)		oe equation, where $n$ is the new rows after Pattern A	ne number of
	or		is 7)	(correct answer
	7 rows added to A		not implied by answer 7	
	6	A1		
	Additional Guidance			
	6 with no incorrect working		M1A1	
	7 or 8 with no working			M0A0
	Multiplication of ratio with no working v eg 10:9 20:18 30:27 40:36	vorthy of N	Л1	M0A0

Question	Answer	Mark	Commer	nts
	Alternative method 1			
	12 ÷ 20 or 0.6(0)	M1	oe	
	their 0.6(0) × 3 ÷ 2 or 0.9(0) or 14.4(0) or 26.4	M1dep	oe	
	26.40	A1	correct money notation	
	Alternative method 2			
	12 × 3 ÷ 2 or 18	M1	oe	
	their 18 ÷ 20 or 0.9(0) or their 18 ÷ 5 × 4 or 14.4(0) or 26.4	M1dep	oe	
	26.40	A1	correct money notation	
	Alternative method 3			
4.4(b)	12 ÷ 5 × 4 or 9.6(0)	M1	oe	
14(D)	their 9.6(0) × 3 ÷ 2 or 14.4(0) or 26.4	M1dep	oe	
	26.40	A1	correct money notation	
	Alternative method 4			
	16 ÷ 2 × 3 or 24 or 44	M1	oe	
	their 24 × 12 ÷ 20 or 14.4(0) or their 44 × 12 ÷ 20 or 26.4	M1dep	oe	
	26.40	A1	correct money notation	
	Ad	ditional G	uidance	
	Condone 26.40p			M1M1A1
	20 ÷ 12 or 1.66 or 1.67 with no wo	rking that	is worthy of M1	M0M0A0
	£18 from using £12 as the cost of one	line (may	give a total of £528)	M1M0A0

Question	Answer	Mark	Comments		
	Alternative method 1				
	0.25 + 0.15 + 0.3 or 0.7	M1	oe eg 1 – 0.05 – 0.05 – 0.2		
	their 0.7 × 200	M1dep	oe implied by $\frac{140}{200}$		
	140	A1			
	Alternative method 2				
	0.25 × 200 or 50 or 0.15 × 200 or 30 or 0.3 × 200 or 60	M1	oe		
15	0.25 × 200 + 0.15 × 200 + 0.3 × 200 or 50 + 30 + 60	M1dep	oe implied by $\frac{140}{200}$		
	140	A1			
	Alternative method 3				
	(0.05 + 0.05 + 0.2) × 200 or 2 × 0.05 × 200 + 0.2 × 200 or 2 × 10 + 40 or 60	M1	oe		
	200 – their 60	M1dep	oe implied by $\frac{140}{200}$		
	140	A1			
	Ad	uidance			
	Ignore attempt to simplify $\frac{140}{200}$		M1M1A0		
	$\frac{140}{200}$ and 140 both on answer line		M1M1A0		
	Do not allow a misread of any probab	ility			

16	5:6	B1	
17	$\frac{x}{\sin 42^\circ} = \frac{15}{\sin 104^\circ}$	B1	

Question	Answer	Mark	Commen	ts
	$\pi \times 10^{2} - \pi \times 7^{2}$ or $100\pi - 49\pi$ or $51\pi$ or $\frac{1}{2} \times \pi \times 10^{2} - \frac{1}{2} \times \pi \times 7^{2}$ or $\frac{1}{2} \times 100\pi - \frac{1}{2} \times 49\pi$ or $\frac{1}{2} \times 51\pi$ or $25.5\pi$	M1	oe implied by $102\pi$ method to work out front faces – must not be part work out volume (× 30) may be taken to be full c	and/or back of a method to ircles
	$2 \times \pi \times 10 \times 30 \text{ or } 600\pi$ or $\frac{1}{2} \times 2 \times \pi \times 10 \times 30 \text{ or } 300\pi$ or $2 \times \pi \times 7 \times 30 \text{ or } 420\pi$ or $\frac{1}{2} \times 2 \times \pi \times 7 \times 30 \text{ or } 210\pi$ or $1020\pi \text{ or } 510\pi$	M1	oe method to work out oute curved surfaces may be taken to be full o 1122 $\pi$ implies M1M1	r and/or inner ircles
18	$\left(\frac{1}{2} \times \pi \times 10^{2} - \frac{1}{2} \times \pi \times 7^{2}\right) \times 2$ + $\frac{1}{2} \times 2 \times \pi \times 10 \times 30$ + $\frac{1}{2} \times 2 \times \pi \times 7 \times 30$ or $2 \times 25.5\pi + 300\pi + 210\pi$ or $561\pi$	M1dep	oe dep on M1M1 correct method to work o back, outer curved and i surfaces	out total of front, nner curved
	2 × 30 × 3 or 180	M1	implied by an answer of $n\pi$ + 180 do not award if 180 is used as $180\pi$	
	$561\pi + 180$	A1		
	Ad	ditional G	uidance	
	150 $\pi$ and 105 $\pi$ implies use of radius for	or curved s	urface areas	max M1M0M0M1A0
	Condone use of [3.14, 3.142] for $\pi$ up	to M1M1M	0M1A0	

Question	Answer	Mark	Commer	nts	
		1	1		
19(a)	300	B2	B1 1100 or 1400 seen		
г					
	4	B1			
19(b)	Additional Guidance				
	Ignore incorrect 'units' eg 4 people			B1	

	Ticks type B and gives valid reason		eg valid reasons	
			and (median for A is) 1260	00
			median for B is 40 more	(than A)
			B1	
			no or incorrect decision and (median for A is) 120 and (median for B is) 130	60 00
		DO	or	
		B2	no or incorrect decision and median for B is 40 m	nore (than A)
19(c)			or	
			ticks type B and (median for B is) 130 and (median for A is) 123	ks type B nd (median for B is) 1300 nd (median for A is) 1230 or 1280
			or	
			ticks type B	
			one median given it mus	t be correct)
	Additional Guidance			
	If median values are not given in the wording, look for values on the graph and box plot			
	Ticks type B but gives no valid reason			B0
	Allow use of average or middle for median, or a correct description eg 'top 50%'. Do not accept 'mean' or 'mode' or other statistical measures for median			
	Ignore comments about measures oth	ner than the	e median	
	Ignore units given in explanation			

Question	Answer	Mark	Commer	nts	
	Alternative method 1				
	$(5^{\text{th}} \text{ term} =) a + 10b + 4b + 4b$ or $(5^{\text{th}} \text{ term} =) a + 18b$	M1	oe		
	a + 6b = 8 and $a + 18b = 44$	M1dep	oe correct simultaneous eg 3a + 18b = 24 and $a + 7implied by 12b = 36 or 2$	equations 18 $b = 44$ 2 $a = -20$	
	b = 3 or $a = -10$	A1			
	a = -10 and $b = 3$	A1			
20	Alternative method 2				
	$(d =) \frac{44 - 8}{3}$ or $(d =) \frac{36}{3}$ or $(d =) 12$	M1	any letter		
	4b = 12	M1dep	oe		
	<i>b</i> = 3	A1			
	a = -10 and $b = 3$	A1			
	Additional Guidance				
	Correct substitution without writing sir first two marks on alt 1	multaneous	s equations scores the		
	eg $(a = 8 - 6b \text{ and}) 8 - 6b + 18b = 44$			M1M1	



22 A U B' B1	
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Question	Answer	Mark	Commer	nts
	Alternative method 1			
	<u>6</u> or <u>3</u> 5 4	M1	oe fractions, decimals or but not $\frac{6}{5}$ as a mixed nu	percentages, Imber
	$\frac{6}{5} \times \frac{3}{4}$ or $\frac{18}{20}$ or $\frac{9}{10}$ or 0.9 or 90% or 0.1 or 10%	M1dep	oe fractions or decimals, mixed number	but not $\frac{6}{5}$ as a
	1 10	A1	oe fraction	
	Alternative method 2			
	Chooses value for price and increases by $\frac{1}{5}$ or chooses number of laptops and decreases by $\frac{1}{4}$	M1	correct method or value eg (£)5 and (£)6 or 20 (laptops) and 15 (lapt	for either ops)
23	Chooses value for price and increases by $\frac{1}{5}$ and chooses number of laptops and decreases by $\frac{1}{4}$	M1dep	correct method or values	3
	and <u>reduction</u> (× 100) or <u>reduction</u> (× 100) or <u>original</u> (× 100)		eg $(x \ 100)$ or $\frac{5 \times 20 - 6 \times 15}{5 \times 20}$ (x 100)	))
	1 10	A1	oe fraction	
	Ad	ditional G	uidance	
	For full marks, accept a fraction equiva	Ilent to 1 10 entage	_ incorrectly simplified, )	M1M1A1 M1M1A0
	If both methods tried and answer incor	rect, awar	d better method mark	
	Accept variables in any working for M1	M1		

Question	Answer	Mark	Commen	its
24(a)	1 16	B3	B2 $2^{-4}$ or $\frac{1}{2^4}$ or $4^{-2}$ or or $0.5^4$ or $\frac{16384}{262144}$ oe f B1 $2^{18}$ or $2^5 \div 2^9$ or $(2^2)^{-2}$ or $4^7 \div 4^9$	$\frac{1}{4^2} \text{ or } 16^{-1}$
24(b)	25 × 25 <sup><math>\frac{1}{2}</math></sup> or $(25^{\frac{1}{2}})^3$ or $(25^3)^{\frac{1}{2}}$ or 25 (x) $\sqrt{25}$ or 25 × 5 or 5 <sup>3</sup> or $\sqrt{25^3}$ or $(\sqrt{25})^3$ or $\sqrt{15625}$ or 15625 <sup><math>\frac{1}{2}</math></sup> or $\sqrt{25 \times 25^2}$ or $\sqrt{25 \times 625}$	M1	oe condone $\pm$ on any $$	
	125	A1		
	Additional Guidance			
	±125			M1A0
25(a)	300	B1		

25(b)	240	B1	

Question	Answer	Mark	Comments		
	Alternative method 1				
	$\frac{4}{5}$ : $\frac{2}{3}$ : 1	M1			
	$\frac{12}{15}$ . $\frac{10}{15}$ . $\frac{15}{15}$	M1dep	oe common denominator implied by correct unsimplified ratio eg 24 : 20 : 30		
	12 : 10 : 15	A1			
	Alternative method 2				
	a:c=4:5 or $b:c=2:3$	M1	oe may be seen as part of a ratio with three values		
	a: c = 12: 15 and $b: c = 10: 15$	M1dep	oe with $c$ values equal		
	12 : 10 : 15	A1			
	Alternative method 3				
26	(5a =) 6b = 4c or $1: \frac{5}{6}: \frac{5}{4}$ or $\frac{6}{5}: 1: \frac{6}{4}$	M1	oe ratio		
	$\frac{12}{12} \cdot \frac{10}{12} \cdot \frac{15}{12} \text{ or } \frac{24}{20} \cdot \frac{20}{20} \cdot \frac{30}{20}$	M1dep	oe common denominator implied by correct unsimplified ratio eg 24 : 20 : 30		
	12 : 10 : 15	A1			
	Alternative method 4				
	Picks values so that $a$ is four fifths of $c$ and $b$ is two thirds of $c$	M1	eg (a =) 60, (b =) 50, (c =) 75 (a =) 4, (b =) $\frac{10}{3}$ , (c =) 5		
	Correct ratio for their values as integers or fractions with a common denominator	M1dep	eg 60:50:75 or $\frac{12}{3}:\frac{10}{3}:\frac{15}{3}$		
	12 : 10 : 15	A1			

Question	Answer	Mark	Comments	
27(a)	Ticks No and gives valid reason	B1	eg valid reasons could use formula could complete the squa could use $\frac{-3 \pm \sqrt{29}}{2}$	ıre
	Additional Guidance			
	Any working or solutions shown must be correct			
	If the quadratic formula is written down it must be correct			
	Ignore irrelevant non-contradictory statements			
	Ticks No and 'There are other methods'			B1
	Ticks No and 'a and b could be decimals'			B1
	Ticks No and 'She could draw a graph'			B1
	Ticks No and 'All quadratic equations can be solved (even if the solutions aren't real numbers)'			B1
	Ticks No and 'The discriminant is positive'			B1
	Ticks No and 'Not all quadratics factorise'			B0
	Ticks No and 'It does factorise'			B0
	Ticks Yes			B0

Question	Answer	Mark	Commer	nts
27(b)	$(x+3)^{2} = \frac{4}{9}$ or $\sqrt{9} (x+3) = (\pm) \sqrt{4}$ or $3(x+3) = (\pm)2$ or $\left( (x+3) + \frac{2}{3} \right) \left( (x+3) - \frac{2}{3} \right)$	M1	Oe	
	$x + 3 = \pm \sqrt{\frac{4}{9}}$ or $3x = \pm 2 - 9$ or $x + 3 = \pm \frac{2}{3}$	M1dep	oe eg $(x =) -3 \pm \sqrt{\frac{4}{9}}$ $(x =) \frac{2}{3} - 3$ and $(x =) -\frac{2}{3} - 3$	
	$-\frac{7}{3}$ and $-\frac{11}{3}$ with correct working for M1M1	A1	allow equivalent fractions decimals or mixed numbe	or recurring rs
	Additional Guidance			
	For up to M1M1, allow 0.66 or 0.67 for $\frac{2}{3}$ and -2.33 for $-\frac{7}{3}$ and -3.66 or -3.67 for $-\frac{11}{3}$			
	Answers -2.33 and -3.66 or -3.67 with correct working			M1M1A0
	$(x =) -\frac{7}{3}$ and $(x =) -\frac{11}{3}$ with no correct working			MOMOAO
	Do not allow incorrect conversion of correct solutions			M1M1A0
	Allow $3(x + 3) = (\pm) 2$ followed by $3x + 9 = (\pm) 2$ etc as a correct method even though it includes a bracket expansion			

Question	Answer	Mark	Commer	nts
	$\frac{14\sqrt{5}}{3}$	B3	oe eg $\frac{28\sqrt{5}}{6}$ B2 $(\sqrt{2\frac{2}{9}} =) \frac{2\sqrt{5}}{3}$ or $(\sqrt{80} =) 4\sqrt{5}$ and $(\sqrt{2\frac{2}{9}} =) \frac{\sqrt{20}}{3}$ or $(\sqrt{2\frac{2}{9}})$ B1 $(\sqrt{80} =) 4\sqrt{5}$ or $(\sqrt{2\frac{2}{9}} -) \frac{\sqrt{20}}{3}$ or $(\sqrt{2\frac{2}{9}})$	$=)\frac{2\sqrt{5}}{\sqrt{9}}$ $\sqrt{2\frac{2}{9}} - 1\frac{2\sqrt{5}}{\sqrt{9}}$
	Additional Guidance			
28	For B1 or B2, allow $\frac{6\sqrt{5}}{9}$ for $\frac{2\sqrt{5}}{3}$ and $\frac{\sqrt{180}}{9}$ for $\frac{\sqrt{20}}{3}$			
	$\frac{14}{3}\sqrt{5}$			B3
	$16\sqrt{5} + \frac{2\sqrt{5}}{3} = \frac{50\sqrt{5}}{3}$			B2
	$4\sqrt{5} + \frac{2\sqrt{5}}{3} + \frac{4^2}{3}\sqrt{5}$			B2
	$4\sqrt{5} + \frac{2\sqrt{5}}{9} = \frac{38\sqrt{5}}{9}$			B1
	$2\sqrt{2} + \frac{\sqrt{20}}{3} = \frac{7\sqrt{20}}{3}$			B1

Question	Answer	Mark	Comments		
29(a)					
	$(x+3)^2 - 1$	M1			
	$x^2 + 3x + 3x + 9 - 1$	M1	oe		
	or $x^2 + 6x + 8$				
	b = 6 and $c = 8$	A1	SC1 $b = 6$ or $c = 8$		
	Alternative method 2				
	$(x-3)^2 + b(x-3) + c = x^2 - 1$	M1			
	$x^2 - 6x + 9 + bx - 3b + c = x^2 - 1$	M1			
	b = 6 and $c = 8$	A1	SC1 $b = 6$ or $c = 8$		
	Alternative method 3				
	(x + 3 + 1)(x + 3 - 1)		difference of two squares		
	or $(x4)(x2)$	M1	from the original roots		
	or $(x + 4)(x + 2)$				
	$x^{2} + 4x + 2x + 8$ or $x^{2} + 6x + 8$	M1			
	b = 6 and $c = 8$	A1	SC1 $b = 6$ or $c = 8$		
	Additional Guidance				
	Working out the roots of the original curve or the translated curve is not enough for M1 in alt 3				

Question	Answer	Mark	Commer	nts	
29(b)	$y = 1 - x^2$ or $y = -x^2 + 1$	B1	oe equation		
	Additional Guidance				
	$-y = x^2 - 1$			B1	
	$y = -(x^2 - 1)$			B1	
	y = -(x - 1)(x + 1)			B1	
	$y = 1 - (-x)^2$			B1	
	$(y = 1 - x^2$ in working with answer) 1	$-x^2$		B0	
	$y = (-x)^2 + 1$			B0	
	$f(x) = 1 - x^2$			B0	
	$\frac{\sqrt{3}}{2} \times \sqrt{3} + \frac{1}{2}$		B2 $\frac{\sqrt{3}}{2} \times \sqrt{3} + \frac{1}{2}$		
	$=\frac{3}{2}+\frac{1}{2}$ B3 B1 cos 30°= $\frac{\sqrt{3}}{2}$ or tan			n 60°= √3	
	= 2		or sin 30°= $\frac{1}{2}$		
	Additional Guidance				
20	For B3 all steps must be shown				
30	Allow $\frac{\sqrt{3}}{2} \times \sqrt{3} + \frac{1}{2}$ given as $\frac{\sqrt{3}}{2} \times \sqrt{3}$ , followed by their $\frac{3}{2} + \frac{1}{2}$				
	Allow equivalent expressions for all trig values				
	eg				
	$\cos 30^\circ = \sqrt{\frac{3}{4}} \sin 30^\circ = \frac{\sqrt{1}}{2}  \tan 60^\circ = \frac{\sqrt{3}}{\sqrt{1}}$				
	For B1 allow the trig value(s) given in a table unless contradicted in working				