

Please write clearly in	ı block capitals.		
Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

GCSE **MATHEMATICS**

H

Higher Tier

Paper 2 Calculator

Thursday 7 June 2018

Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- · The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

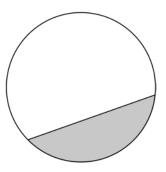
Advice

• In all calculations, show clearly how you work out your answer.

For Exam	iner's Use
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
26–27	
28–29	
TOTAL	

Answer all questions in the spaces provided

1 Here is a circle.



Circle the word that describes the shaded part.

[1 mark]

segment

chord

sector

arc

Circle the number that is in standard form. 2

[1 mark]

$$0.25 \times 10^4$$
 6×10^7 38×10^{-3} $4 \times 10^{\frac{1}{2}}$

$$6 \times 10^{7}$$

$$38 \times 10^{-3}$$

$$4 \times 10^{\frac{1}{2}}$$

3 $y \text{ is } 1\frac{1}{2} \text{ times } x.$

Circle the ratio that is equivalent to y: x

[1 mark]

- 2:5
- 5:2
- 3:2
- 2:3

Work out 40 as a percentage of 10 Circle your answer.

[1 mark]

4%

25%

300%

400%

Turn over for the next question

5	Match each sequence to its description. One has been done for you.	[4 marks]
	1 1 2 3 5 8	Arithmetic progression
	1 2 4 8 16 32	Geometric progression
	1 2 3 4 5 6	Fibonacci sequence
	1 3 6 10 15 21	Triangular numbers
	1 4 9 16 25 36	Cube numbers
	1 8 27 64 125 216	Square numbers

6	The table shows information about the population of a city.	
U	The table shows information about the population of a city.	

Population in 2001	Population in 2011
420 000	480 000

Liam claims,

"From 2011 to 2021 the population of the city will increase by the same percentage as from 2001 to 2011"

He works out,

population increase from 2001 to 2011 =
$$480\ 000 - 420\ 000$$

= $60\ 000$

population in
$$2021 = 480\ 000 + 60\ 000$$

= $540\ 000$

Does the population of 540 000 match his claim?

Answer

You must sho	w your	working.
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,	o .		[3 marks]

Turn over for the next question

7	On three days, Ali throws darts at a target.
	Here are his results

	Number of throws	Number of hits	Number of misses
Monday	20	15	5
Tuesday	30	22	8
Wednesday	40	17	23
Total	90	54	36

7	(a)	Work out two different estimates for the probability of Ali hitting the target.	[2 marks]
		Answer and	
7	(b)	Which of your two answers is the better estimate for the probability of Ali hitting	ı the
		target?	
		Give a reason for your answer.	[1 mark]
		Answer	
		Reason	

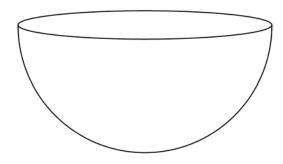
8	Theo starts with savings of £18 James starts with no savings.		
	Each week from now,		
	Theo will save £4.50 and James will save £4		
	In how many weeks will Theo and James have savings in the ratio 15:8?	[3 marks]	
	Answer		

9		The length of each side of a regular pentagon is 8.4 cm to 1 decimal place.	
9	(a)	Complete the error interval for the length of one side.	[2 marks]
		cm ≼ length < cm	
9	(b)	Complete the error interval for the perimeter.	[1 mark]
		cm ≤ perimeter < cm	1

10

Volume of a sphere = $\frac{4}{3}\pi r^3$ where r is the radius

A container is a hemisphere of radius 30 cm



Sand fills the container at a rate of 4000 cm³ per minute.

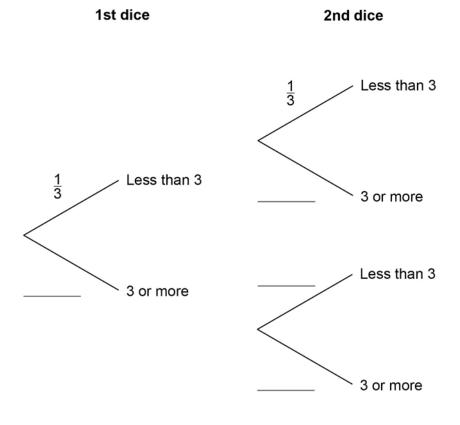
Does it take **less than** a quarter of an hour to fill the container? You **must** show your working.

•	J		[3 marks]

Answer _____

- 11 Two ordinary fair dice are rolled.
- 11 (a) Complete the tree diagram.

[1 mark]



11 (b) Work out the probability that **both** dice land on a number less than 3

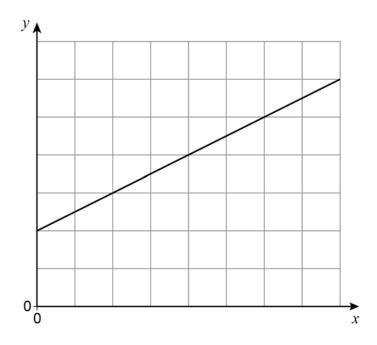
[1 mark]

Answer

s]	Do not write outside the box

11	Work out the probability that exactly one of the dice lands on a number less t	
		[2 marks]
	Answer	
	Turn over for the next question	
	, , , , , , , , , ,	

12 A straight line is drawn on the centimetre grid.



Fay assumes that the scale is 1 cm represents 1 unit.

12 (a) Use her assumption to work out the gradient of the line.

[1 mark]

Answer

12 (b)	In fact, the scale is 1 cm represents 2 units.	Do not write outside the box
	Which statement is correct?	
	Tick one box. [1 ma	rk]
	The answer to part (a) is too big	
	The answer to part (a) stays the same	
	The answer to part (a) is too small	
	Turn over for the next question	
		2

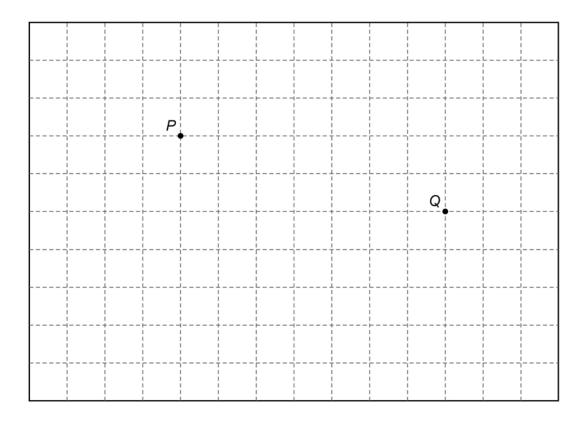
$\frac{8x^2 - 8}{4x + 4}$ simplifies to the form $ax + b$ where a and b are integers.	$\frac{8x^2 - 8}{4x + 4}$ simplifies to the form $ax + b$ where a and b are integers [5]	Show that	for $x \neq -$	1		
		$\frac{8}{4}$	$\frac{x^2-8}{x+4}$	simplifies to the form	ax + b	where a and b are integ

14 The scale drawing represents a garden.

Water from a sprinkler at P reaches up to 20 metres from P.

Water from a sprinkler at Q reaches up to 25 metres from Q.

Scale: 1 cm represents 5 m



Using a pair of compasses,

show the region that water from **both** sprinklers reaches.

[2 marks]

Turn over for the next question

15 100 men and 100 women took a test.

Scores

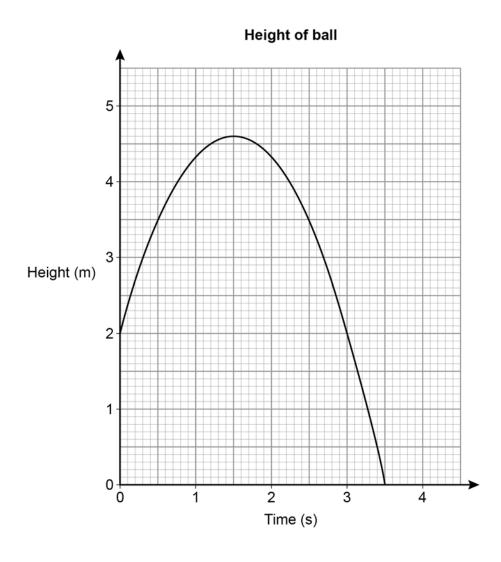
	Median	Interquartile range	Range
Men	28	7.5	31
Women	30	9	37

Using this data, which statement **must** be true? Tick **one** box. [1 mark] Men had a higher average score than women Men had more consistent scores than women A woman had the highest score A man had the lowest score

16		Some concrete has volume 3.8 m ³			outside to
16	(a)	The density of the concrete is 2400 kg/m ³			
		Work out the mass of the concrete.		[2 marks]	
		Answer	kg		
16	(b)	The 3.8 m³ of concrete is made into the shape of a cylinder. The base has radius 0.5 metres.			
		Work out the height of the cylinder.		[2 marks]	
		Answer	m		
					5

17 A ball is thrown vertically upwards.

The graph shows the height of the ball above the ground after it is thrown.



17 (a) For how many seconds is the ball at a height of **more than** 2 metres?

[1 mark]

Answer____s

17 (b) After how many seconds is the ball at instantaneous rest when it is in the air?

[1 mark]

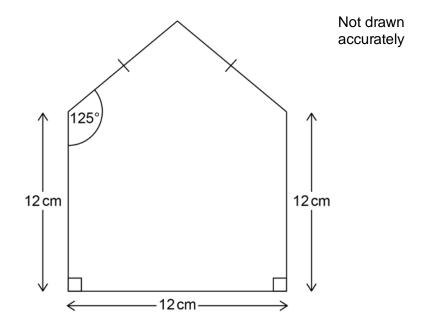
Answer____s

ownwards.	[2 marks]	Do not write outside the box
m/s		
utive integers.	[1 mark]	

17 (c)	Work out the average speed of the ball when it is moving downwards.	[2 marks]
	Answer m/s	
18	The solution of $3^x = 300$ lies between two consecutive integers. Work out the two integers.	
		[1 mark]
	Answer and	
	Turn over for the next question	

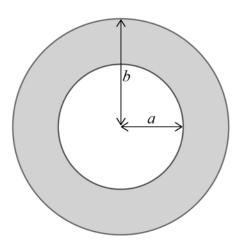
19 A pentagon is made from a square and an isosceles triangle.

Answer _



work out the perimeter of the pentagon.	[4 marks]

20 Here is an inflated swimming ring with dimensions in centimetres.



The volume of the ring, $V \, \mathrm{cm}^3$, is given by

$$V = 0.25\pi^2(b-a)^2(b+a)$$

Work out the volume when a = 20 and b = 30Give your answer to 3 significant figures.

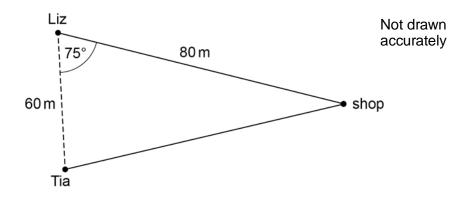
[3 marks]

Answer _____ cm³

Turn over for the next question

Liz and Tia are walking towards a shop along different straight paths.

The diagram shows their positions at 2 pm



21 (a) Assume they walk at the same speed.

Who will arrive at the shop first?

You **must** show your working.

[3 marks]

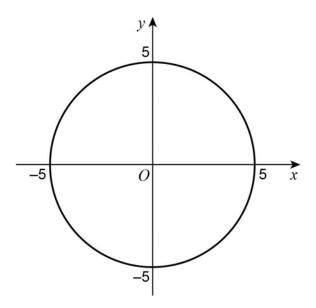
Answer

21 (b) In fact, Liz walks at a faster speed than Tia.

How does this affect the answer to part (a)?

[1 mark]

22 A circle, centre O, passes through (5, 0).



What is the equation of the circle? Circle your answer.

[1 mark]

$$x^2 + y^2 = 25$$

$$x^2 + y^2 = 5$$

$$x^2 + y^2 = 10$$

$$x^{2} + y^{2} = 25$$
 $x^{2} + y^{2} = 5$ $x^{2} + y^{2} = 10$ $x^{2} + y^{2} = 100$

Turn over for the next question

Do not write outside the box

23	Solids X and Y are similar. X has volume 64 cm ³ Y has volume 343 cm ³	
	The surface area of X is 176 cm ²	
	Work out the surface area of Y.	
		[3 marks]
	Answer	cm ²

A tank is a cuboid measuring 50 cm by 35 cm by 20 cm All lengths are to the nearest centimetre .	
A container has a capacity of exactly 34 litres. 1 litre = 1000 cm ³	
Which has the greater capacity? Tick one box.	
Tank Container Cannot tell	
Show working to support your answer. [4 marks]
	_
	_
	_ _
	_
	_
Turn over for the next question	

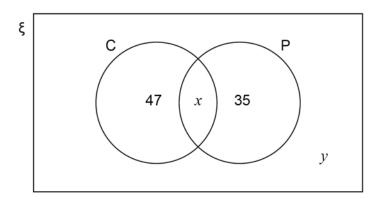
25 The Venn diagram shows some information about 150 students.

 ξ = 150 students

C = students who study Chemistry

Answer

P = students who study Physics



The probability that a Physics student, chosen at random, also studies Chemistry is $\frac{5}{12}$ One of the 150 students is chosen at random.

Work out the probability that the student does **not** study either Chemistry or Physics.

[4 marks]

26	A curve has equation $y = 4x^2 + 5x + 3$ A line has equation $y = x + 2$		c
	Show that the curve and the line have exactly one por Do not use a graphical method.	pint of intersection.	
		[4 marks]	
	Turn over for the next questi	on	
			_

27	Prove algebraically that	2.75	converts to the fraction	124 45	[3 marks]

Do not write outside the box

28		f(x) = 5 - x and $g(x) = 3x + 7$	O		
28	(a)	Simplify $f(2x) + g(x-1)$	[3 marks]		
		Answer			
28	(b)	Solve $g^{-1}(x) = 2x$	[3 marks]		
		x =			
	END OF QUESTIONS				

