AQA

GCSE
MATHEMATICS

H

Higher Tier   Paper 3 Calculator

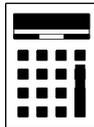Tuesday 12 June 2018   Morning   Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:
- a calculator
- mathematical instruments.

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Advice

- In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24–25	
TOTAL	

Do not write outside the box

Answer all questions in the spaces provided

1   Circle the decimal that is closest in value to $\dfrac{11}{20}$

[1 mark]

0.56   0.6   0.525   0.5

2   Circle the list of **all** the integers that satisfy $-2 < x \leqslant 4$

[1 mark]

−2, −1, 0, 1, 2, 3   −1, 0, 1, 2, 3

−2, −1, 0, 1, 2, 3, 4   −1, 0, 1, 2, 3, 4

3   Circle the largest number.

[1 mark]

$3.2\dot{7}$ 3.27   3.277 $3.20\dot{7}$

4   What is the size of an exterior angle of a regular decagon?

Circle your answer.

[1 mark]

18°   36°   144°   162°

5 a is a common factor of 72 and 120

b is a common multiple of 6 and 9

Work out the highest possible value of $\dfrac{a}{b}$

[4 marks]

_____

_____

_____

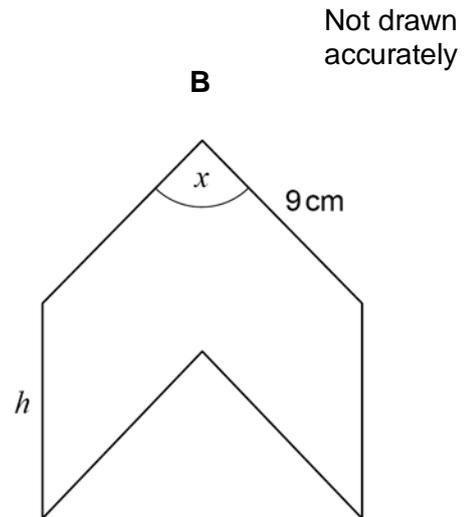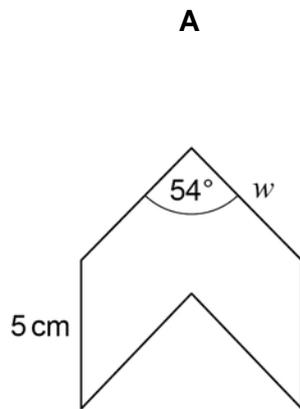_____

_____

_____

_____

Answer _____

Turn over for the next question

Turn over ▶

6 A and B are similar shapes.

B is an enlargement of A with scale factor 1.5

Not drawn accurately

A **B**

Work out the values of x, h and w.

[3 marks]

_____

_____

_____

_____

_____

_____

$x =$ _____ degrees

$h =$ _____ cm

$w =$ _____ cm

7

Investment A   Save £150 per month for 2 years.

2.5% interest is added to the total amount saved.

Investment B   Invest £3500

Compound interest is added at 3% per year.

After 2 years, how much **more** is investment B worth than investment A?

[4 marks]

_____

_____

_____

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_____

_____

Answer   £_____

Turn over for the next question

8 (a) Show that the lines $y = 3x + 7$ and $2y - 6x = 8$ are parallel.

Do **not** use a graphical method.

[3 marks]

_____

_____

_____

_____

_____

_____

8 (b) Is the point (–5, –6) above, below or on the line $y = 3x + 7$?

Tick **one** box.

☐ Above ☐ Below ☐ On the line

You **must** show your working.

Do **not** use a graphical method.

[2 marks]

_____

_____

_____

_____

_____

_____

9 The cost of a ticket increases by 10% to £19.25

Work out the original cost.

[3 marks]

Answer £_____

10 The nth term of a sequence is $12n - 5$

Work out the numbers in the sequence that

have two digits

and

are **not** prime.

[3 marks]

Answer _____

11

Turn over ►

11 $a = \begin{pmatrix} 6 \\ -10 \end{pmatrix}$ $b = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$ $c = \begin{pmatrix} -4 \\ 7 \end{pmatrix}$

11 (a)   Work out $a + b + c$

[2 marks]

Answer $\begin{pmatrix} \\ \end{pmatrix}$

11 (b)   Show that $a + 2c$ is parallel to b

[2 marks]

12

$$pressure = \frac{force}{area}$$

A force of 40 Newtons is applied to an area of 3.2 square metres.

Work out the pressure.

Give the units of your answer.

[2 marks]

_____

_____

Answer _____

13 Tick **all** the statements that are true for any rhombus.

[1 mark]

☐ The diagonals are lines of symmetry

☐ The diagonals bisect each other

☐ The diagonals are perpendicular

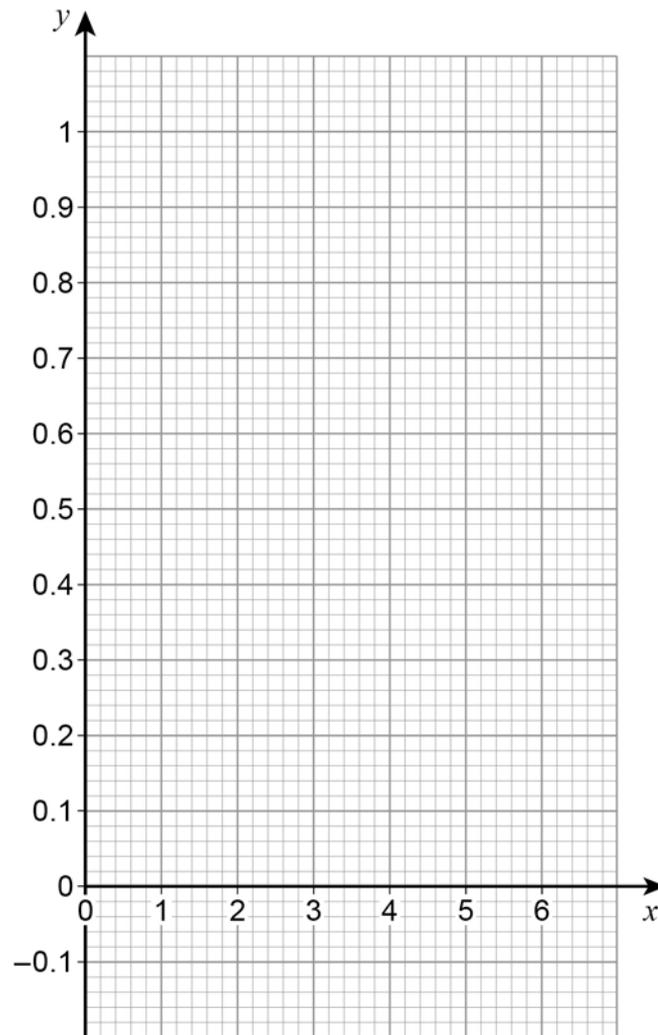☐ The diagonals are equal in length

Turn over for the next question

7

Turn over ▶

14 Draw the graph of $y = 0.8^x$ for values of x from 0 to 6

[3 marks]

x	0	1	2	3	4	5	6
y							

15 Amy has x beads.

Billy has three more beads than Amy.

Carly has four times as many beads as Billy.

Circle the expression for the number of beads that Carly has.
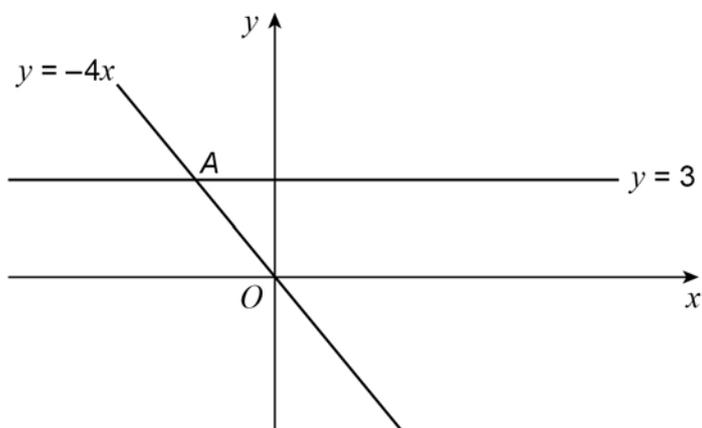
[1 mark]

$4x + 3$ $3x + 4$ $4(x + 3)$ $x + 12$

16 Two straight lines intersect at point A.

$y = -4x$

A

$y = 3$

O

Not drawn
accurately

Circle the coordinates of A.

[1 mark]

$(-\dfrac{3}{4}, 3)$ $(-4, 3)$ $(-12, 3)$ $(-\dfrac{4}{3}, 3)$

Turn over ▶

17 Here are two methods to make a 4-digit code.

Codes can have repeated digits.

Method A

For the first two digits use an odd number between 30 and 100

For the last two digits use a multiple of 11

Method B

Use four digits in the order   even   odd   even   odd

Do **not** use the digit zero

Which method gives the **greater** number of possible codes?
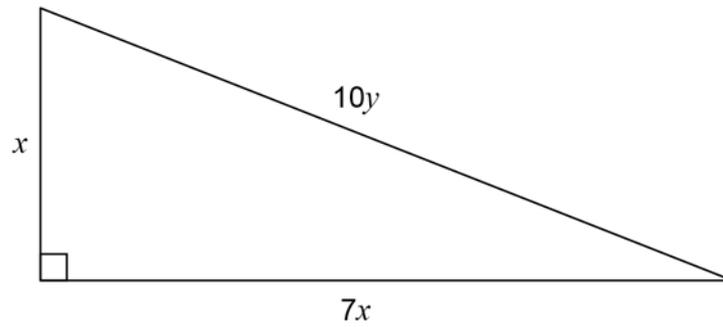
You **must** show your working.

[3 marks]

Answer _____

18 Show that, for $x \neq 0$

$$\frac{x+4}{3x} - \frac{5}{2x}$$

can be written in the form $\frac{ax+b}{cx}$ where a, b and c are integers.

[3 marks]

_____

_____

_____

_____

_____

_____

_____

_____

_____

_____

Answer _____

19 The equation of a straight line is $3x + 2y = 24$

Circle the point where the line crosses the x-axis.

[1 mark]

(0, 8) (12, 0) (0, 12) (8, 0)

Turn over ▶

20 All dimensions are in centimetres.

Not drawn
accurately

$10y$

x

$7x$

Use Pythagoras' theorem to work out the exact value of $\dfrac{x}{y}$

[3 marks]

_____

_____

_____

_____

_____

_____

_____

_____

_____

_____

Answer _____

21 The mass of an ornament is m grams.

The height of the ornament is h centimetres.

m is directly proportional to the cube of h.

$m = 1600$ when $h = 8$

21 (a) Work out an equation connecting m and h.

[3 marks]

Answer

21 (b) Work out the mass of an ornament of height 12 centimetres.

[2 marks]

Answer _____ grams

Turn over for the next question

8

Turn over ▶

22   *A*, *B* and *C* are points on a circle.

DCB is a straight line.

PAQ is a tangent to the circle.

Not drawn accurately
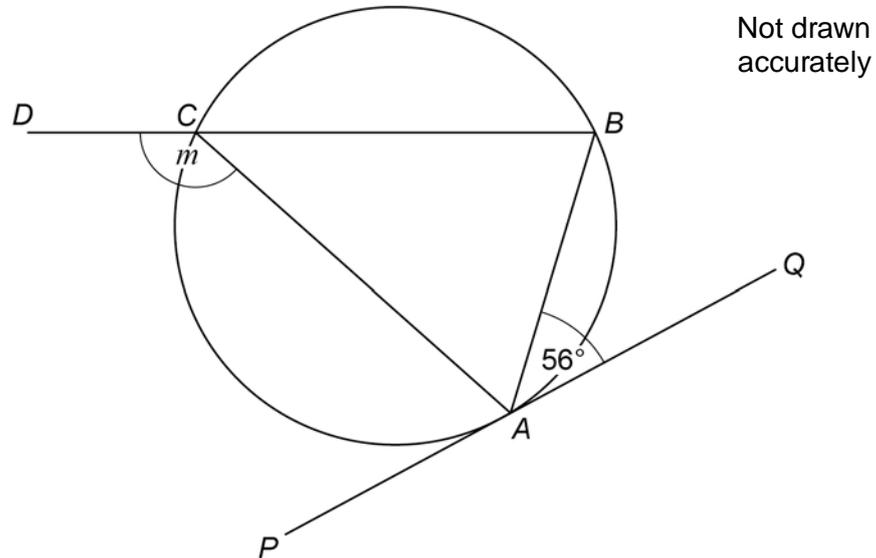
Sam is trying to work out the size of angle m.

Here is his working.

angle $ACB = 56°$	angles in the same segment are equal
$m = 180° - 56°$	angles at a point on a straight line add up to 180°
$m = 124°$	

Make a criticism of his working.

[1 mark]

_____

_____

23 A sequence of numbers is formed by the iterative process

$$u_{n+1} = \frac{3}{u_n + 1}, \qquad u_1 = 4$$

Work out the values of u_2 and u_3

[2 marks]

$u_2 =$

$u_3 =$

Turn over for the next question

3

Turn over ▶

24 The speed-time graph shows 20 seconds of a car journey.

Harry wants to estimate the distance the car travels in this time.

He uses a triangle and a trapezium, as shown, to estimate the area under the graph.

Car journey
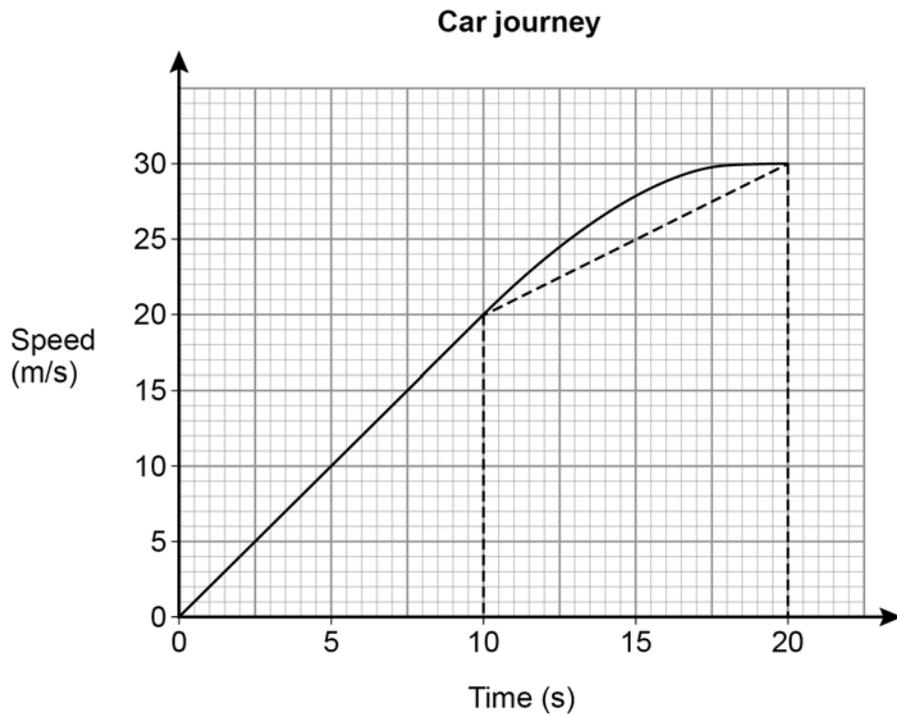
24 (a) Complete Harry's method to estimate the distance the car travels.

[3 marks]

Answer _____ m

24 (b) For this journey, which of these is true for Harry's method?

Tick **one** box.

[1 mark]

It works out an overestimate of the distance

It works out an underestimate of the distance

It could work out an overestimate or an underestimate of the distance

Turn over for the next question

4

Turn over ▶

25   *ABCDEF* is a triangular prism which represents part of a hill.

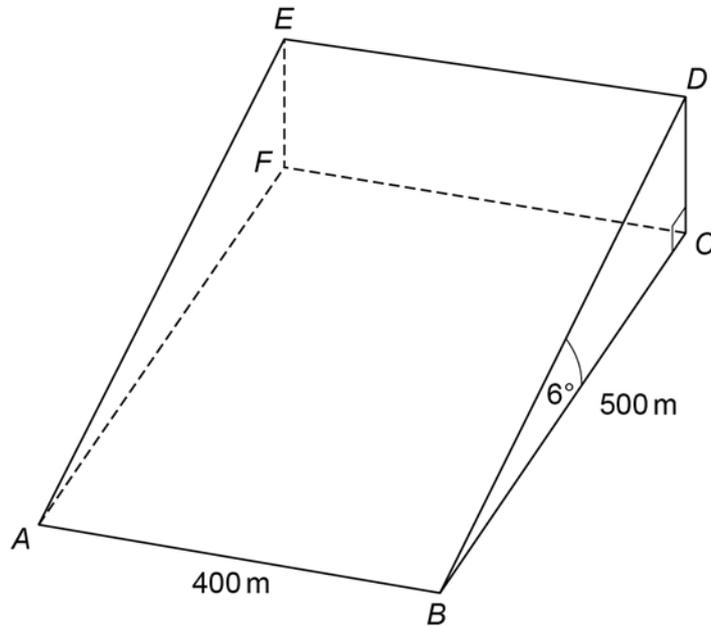*ABCF* is the horizontal rectangular base.

D is vertically above *C*.
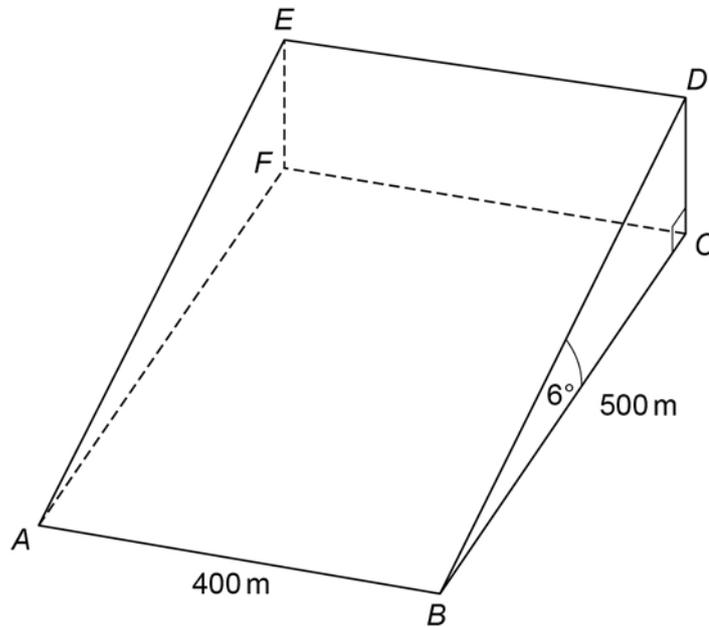
25 (a)   Work out the height *CD*.

[2 marks]

Answer .... m

25 (b) Jamil walks in a straight line from *A* to *D*.

Work out the size of angle *DAC*.

You **must** show your working.

[4 marks]

Answer _____ degrees

6

Turn over ▶

26 The histogram shows information about the speed of cars as they pass a checkpoint.

The scale on the frequency density axis is missing.

Speed of cars

Frequency density

Speed (mph)
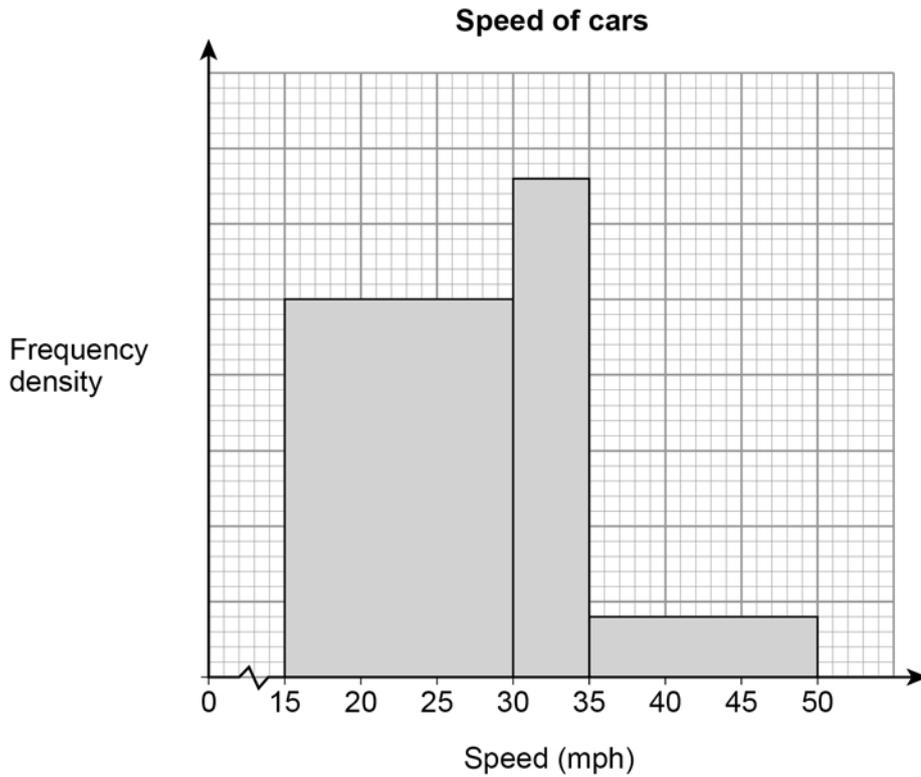
The histogram shows information about 480 cars.

26 (a) How many cars does the first bar represent?

[4 marks]

Answer

26 (b) Cars with a speed greater than 40 mph are over the speed limit.

Use the histogram to estimate the number of cars that are over the speed limit.

[2 marks]

Answer

Turn over for the next question

6

Turn over ▶

27 A bag contains 30 discs.

10 are red and 20 are blue.

One disc is taken out at random and replaced by **two** of the other colour.

Another disc is then taken out at random and replaced by **two** of the other colour.

Another disc is then taken out at random.

Work out the probability that all three discs taken out are **red**.

[3 marks]

Answer _____

28 *P* is a point on the circle with equation $x^2 + y^2 = 80$

P has *x*-coordinate 4 and is below the *x*-axis.

Not drawn accurately

Work out the equation of the tangent to the circle at *P*.

[5 marks]

Answer _____

END OF QUESTIONS

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